

---

# **Integrated Arrayed Waveguide Grating Spectrometers for On-chip Optical Coherence Tomography and Raman Spectroscopy**

---

**B.Imran Akca, N. Ismail, F. Sun, A. Driessen,  
K. Wörhoff, M. Pollnau, and R.M. de Ridder**

Integrated Optical Microsystems Group,  
MESA+ Institute for Nanotechnology,  
University of Twente,  
Enschede,NL

**V.Duc Nguyen, J. Kalkman, and  
T.G. van Leeuwen**

Biomedical Engineering & Physics,  
Academic Medical Center,  
University of Amsterdam  
Amsterdam,NL

# Outline

- ▶ Guided Wave Optics
- ▶ Motivation
- ▶ Arrayed Waveguide Grating (AWG) Spectrometer Design for
  - On-chip Optical Coherence Tomography (OCT) Systems
  - Integrated Raman Spectroscopy
- ▶ Conclusions

# Guided wave theory

**Optical waveguide:** A physical structure for confining and guiding electromagnetic waves spatially.

→ Guiding mechanism: **total internal reflection (TIR)**  $\theta < \cos^{-1}(n_2 / n_1)$

→ Wave guiding condition:

$$2dn_1k_0 \cos(\theta) - 2\varphi_s - 2\varphi_c = m2\pi \quad (m = 0, 1, 2, \dots)$$

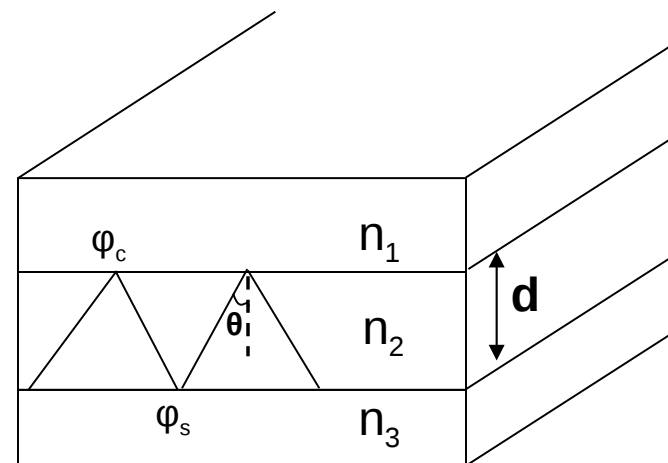
- m: mode number
- $k_0 d$  increase → number of modes increase

→ Longitudinal propagation constant:

$$\beta = k_0 n_2 \sin(\theta)$$

→ Effective refractive index:

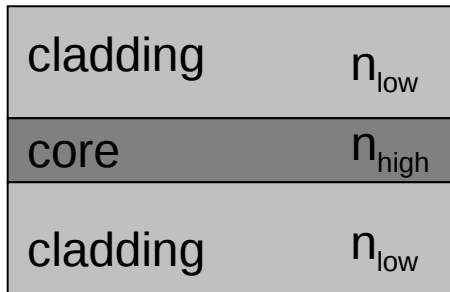
$$\beta / k_0 = n_2 \sin(\theta)$$



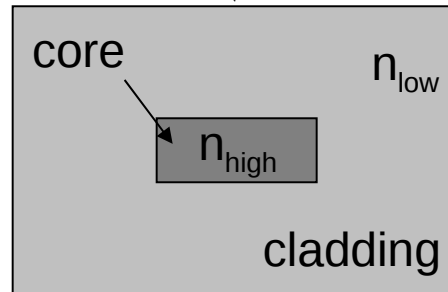
$$n_2 > n_1, n_2 > n_3$$

# Waveguide geometries

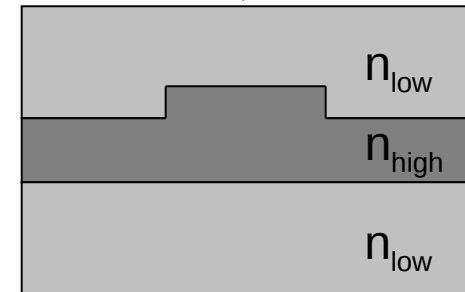
## 1-d optical confinement



Slab waveguide

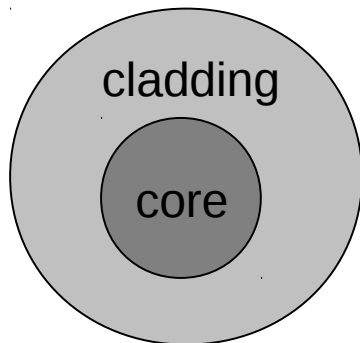


Channel/photonic wire waveguide

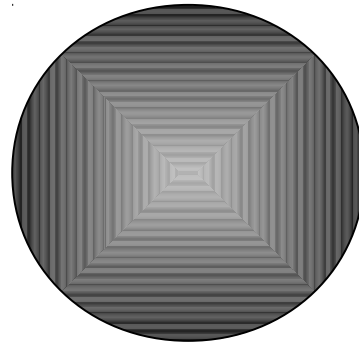


Rib/ridge waveguide

## 2-d optical confinement



Step-index fiber



Graded-index (GRIN) fiber

- Wave approach to waveguides:**
- One-dimensional planar waveguide: harmonic plane waves ( $E(x,t) = A \cos[(kx - wt) - \theta]$ )
  - Rectangular waveguide: analytic solution does not exist
  - Circular waveguide: Bessel functions
  - Circular waveguide with parabolic  $n$ -profile: Gaussian beams ( $E(r) = E_0 e^{-(r/w)^2}$ )

# 1-d optical conf waveguide

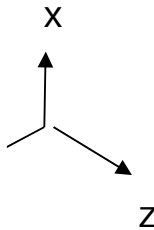
Helmholtz equation:



TE solutions:

$$\vec{E} = \hat{y} E_0 U(x, y) e^{-j\beta z}$$

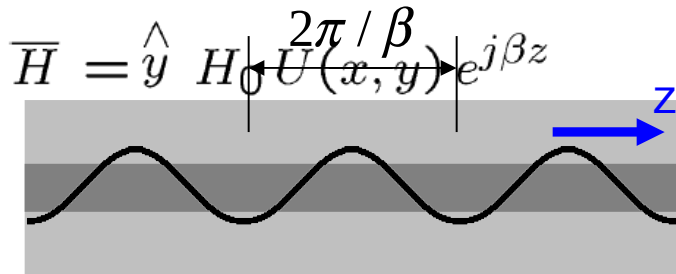
TM solution



Solutions:

$$\vec{E} = \hat{y} E_0 U(x, y) e^{-j\beta z}$$

Solutions:



$$\vec{H} = \hat{y} H_0 U(x, y) e^{-j\beta z}$$

$$\rightarrow U_1 = B e^{\gamma x} \quad \gamma^2 = \beta^2 - k_o^2 n_1^2 \text{ Decaying}$$

$$\rightarrow U_2 = A \cos k_x x \quad k_x^2 = k_o^2 n_2^2 - \beta^2 \text{ Propagating}$$

$$\rightarrow U_3 = B e^{-\gamma x} \quad \gamma^2 = \beta^2 - k_o^2 n_3^2 \text{ Decaying}$$

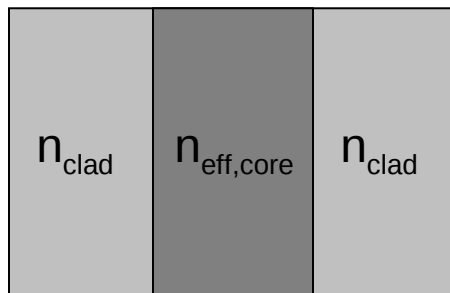
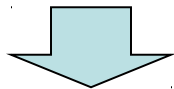
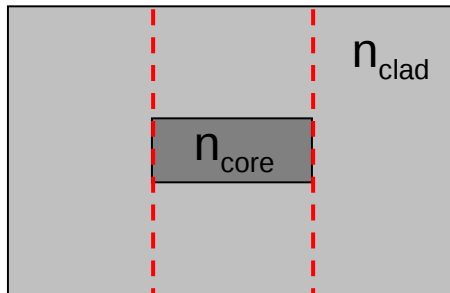
Propagation constant is related to the wavelength (spatial periodicity) of light propagating in the waveguide

$$k = n k_0 = n 2\pi / \lambda \quad \text{effective index} \quad \text{Propagation constant: } \beta = n_{\text{eff}} k_0$$

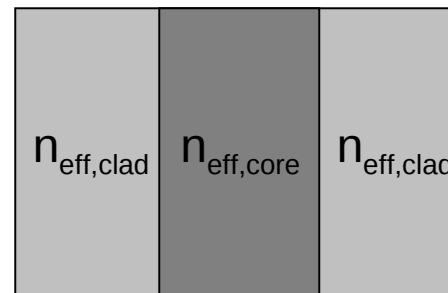
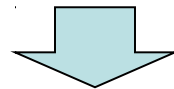
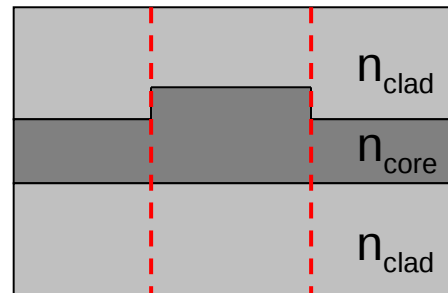
**Confinement in one direction → Little practical application**

# 2-d confinement & effective index method

Channel waveguide



Rib/ridge waveguide



- ◆ Directly solving 2-d Helmholtz equation for  $U(x,y)$
- ◆ Deconvoluting the 2-d equation into two 1-d problems
  - Separation of variables
  - Solve for  $U'(x)$  &  $U''(y)$
  - $U(x,y) \sim U'(x) U''(y)$
- ◆ Less accurate for high-index-contrast waveguide systems
- ◆ Computationally very efficient

TM (TE) Equations



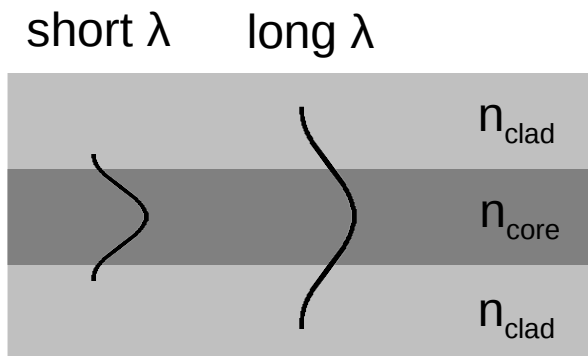
TE (TM) Equations



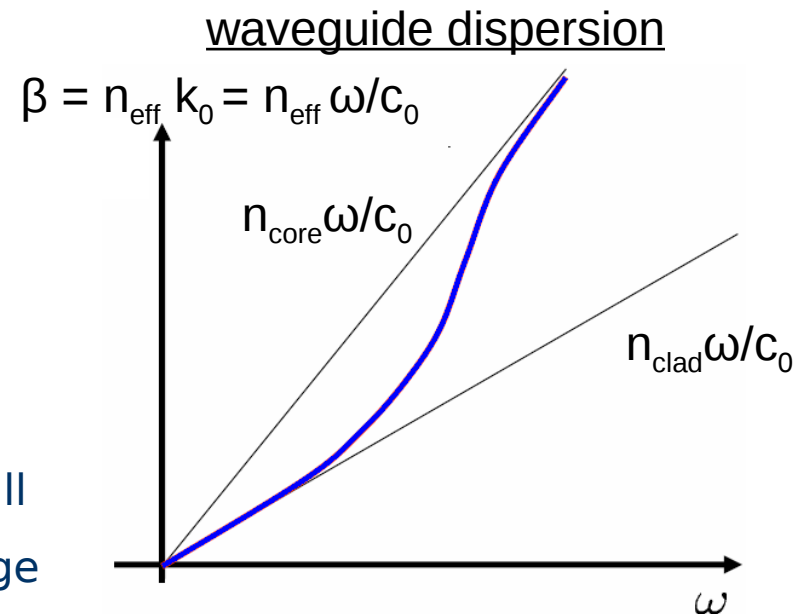
$n^{\text{TM(TE)}}$

# Dispersion: The Basics

- ◆ In optics, **dispersion** is the phenomenon in which the phase /group velocity of a wave depends on its frequency.
- ◆ Dispersion is a measure of the separation between diffracted light of different wavelengths.
- ◆ Caused by Sources, Waveguide Geometry, Materials, Differences in Mode Propagation



- ◆ At long wavelength, effective index is small
- ◆ At short wavelength, effective index is large



# Dispersion:Types

## ◆ **Modal dispersion:**

In multimode waveguides as a result of the differences in the group velocities of the various modes

## ◆ **Waveguide dispersion**

Propagation constant depends on the wavelength even for single mode waveguides

## ◆ **Material dispersion:**

The wavelength dependence of a material's refractive index  
(i.e. the separation of colors in a prism)



# Other aspects of Waveguides

## ◆ Single mode operation

The number of confined modes, and the shape of modes are a function of:

- $\Delta n$  (core/ cladding)
- Waveguide **dimensions (height for slab waveguide)**
- Operation **wavelength**

## ◆ Low Loss

- Essential for all optical waveguides.
- Mostly, fabrication dependent (impurities, roughness)
- Scattering losses due to sidewall roughness is significant.
- Bending losses.

## ◆ Low birefringence

$$\Delta n = n_{te} - n_{tm}$$



- Important for devices which needs to be polarization insensitive.