



Periodic multilayers and FEL radiation

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Free electron laser (FEL)

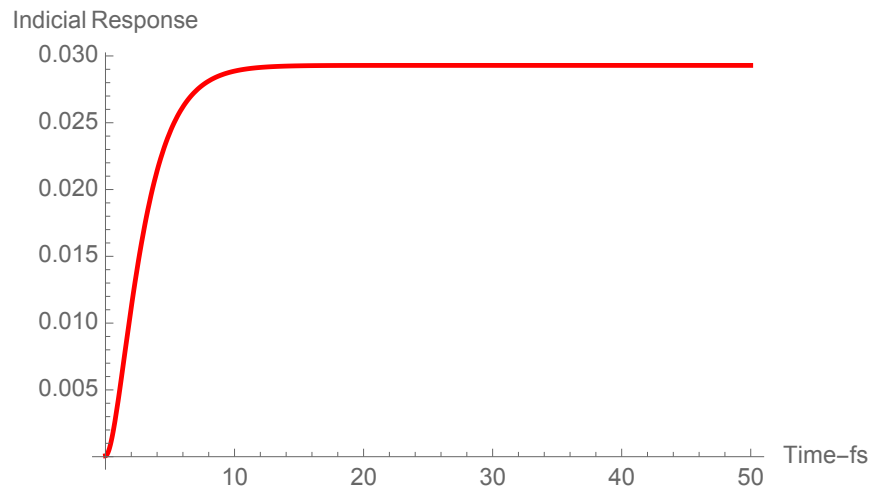
- New facilities around the world (Europe, USA, Japan)
- Very intense ($10^{13} - 10^{15}$ photons per pulse)
- Very short pulse (10 – 100 fs)
- Wide range of wavelengths available (EUV, soft x-ray, hard x-ray)
- Time-dependence of the Bragg diffraction by a multilayer of nanometer period
- Distributed feedback laser (DFB) with a periodic multilayer

Time-dependence

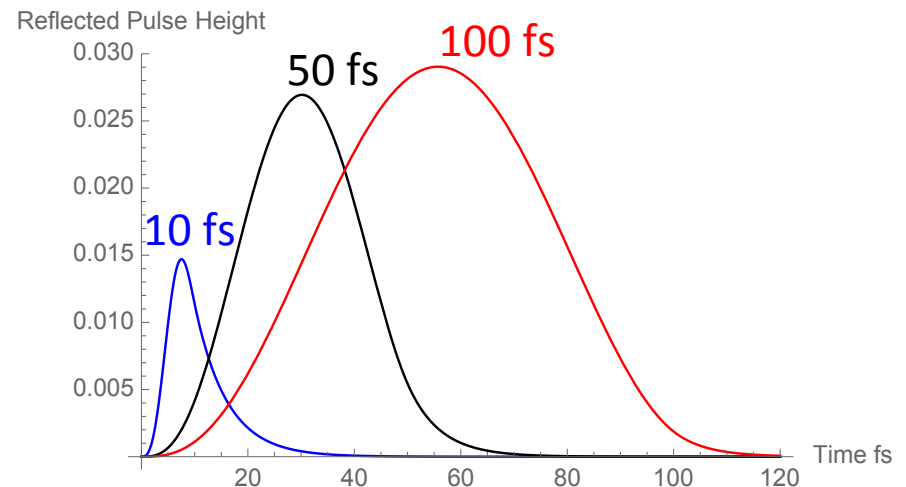
- Propagation of a **single** ultra-short pulse within a one-dimensional photonic crystal
- Linear behaviour of the medium:
no non-linear effect coming from the high incoming intensity
- Time-dependent coupled-wave theory
- Calculation in the time domain

Time-dependence

- Ti/Si multilayer: [Ti (35 nm) /Si (35 nm)]x7
- Photon energy: 20 eV
- Pulse: sine-square function, various pulse lengths
- Diffraction angle: 60°



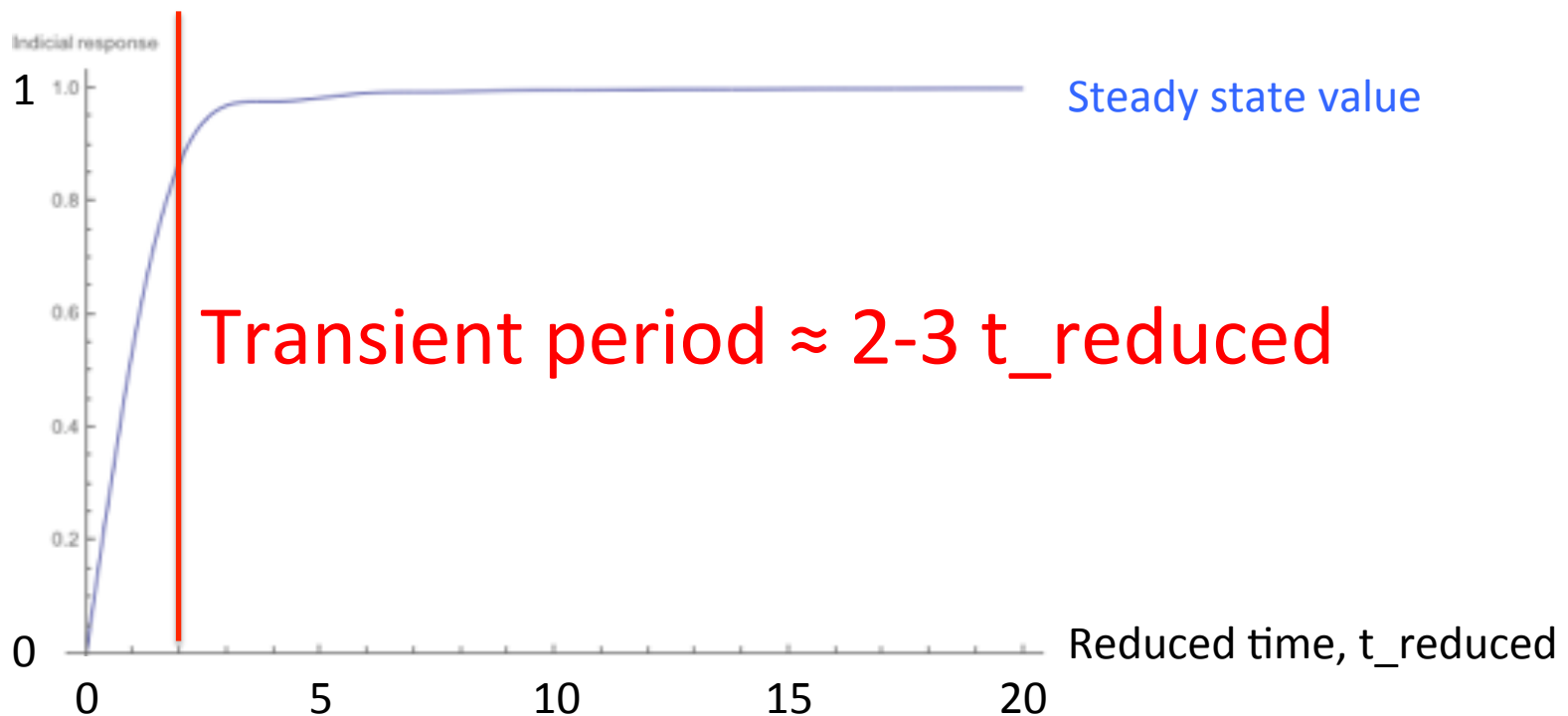
Indicial response



Pulse response

Time-dependence

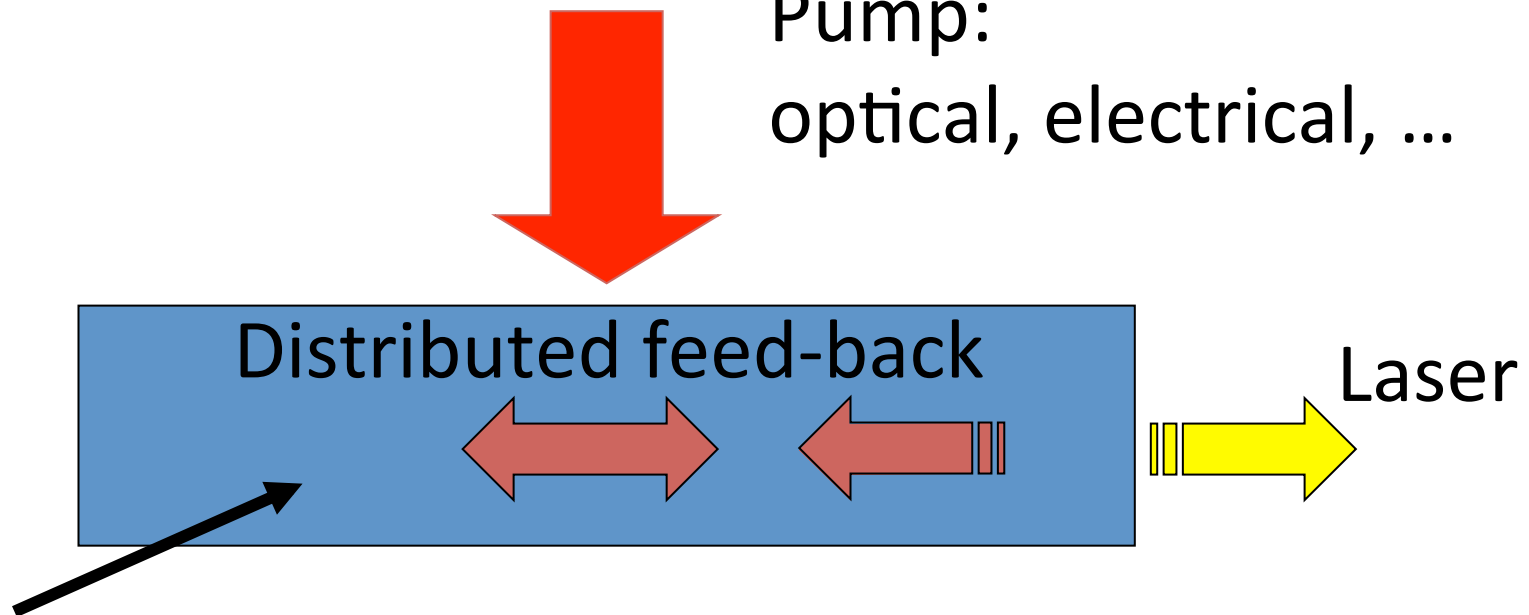
Universal indicial response:
peak reflectance vs reduced time



$$t_{reduced} = t \frac{\pi \sin \theta c}{\Lambda} \text{ with } \Lambda \text{ the extinction length}$$

DFB laser

Pump:
optical, electrical, ...



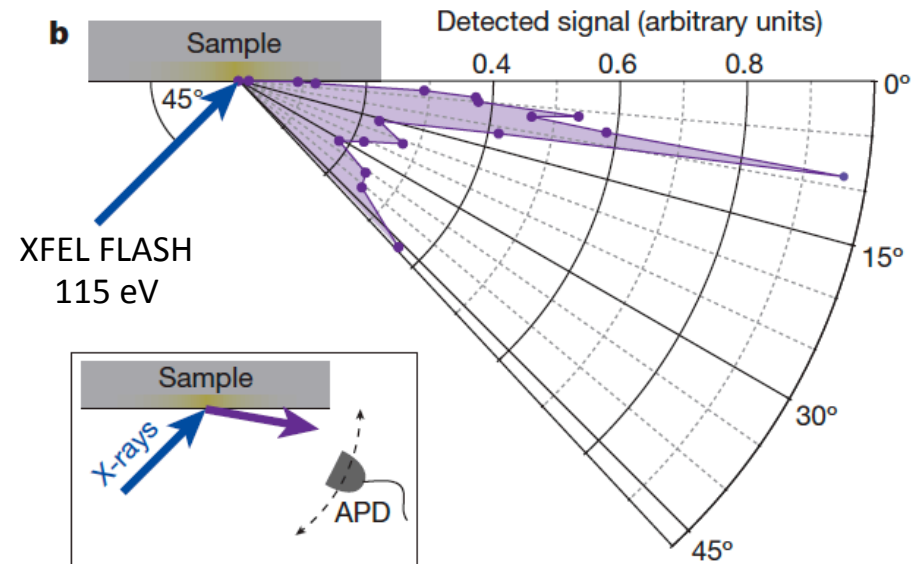
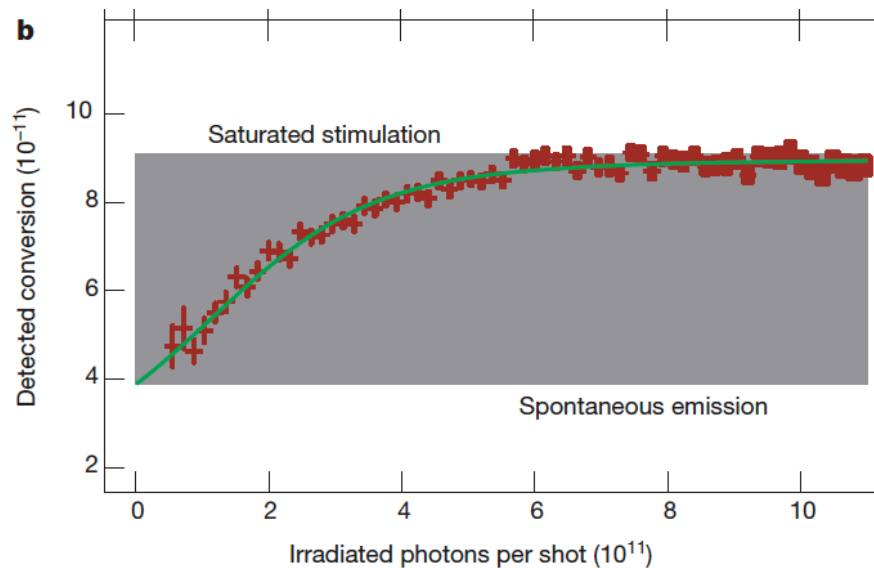
Resonant cavity =

- periodic medium: crystal / Fabry-Pérot / Bragg mirror
- +
• active medium necessary for stimulated emission

No external mirrors, no alignment

DFB laser

X-ray stimulated emission in a solid (silicon)



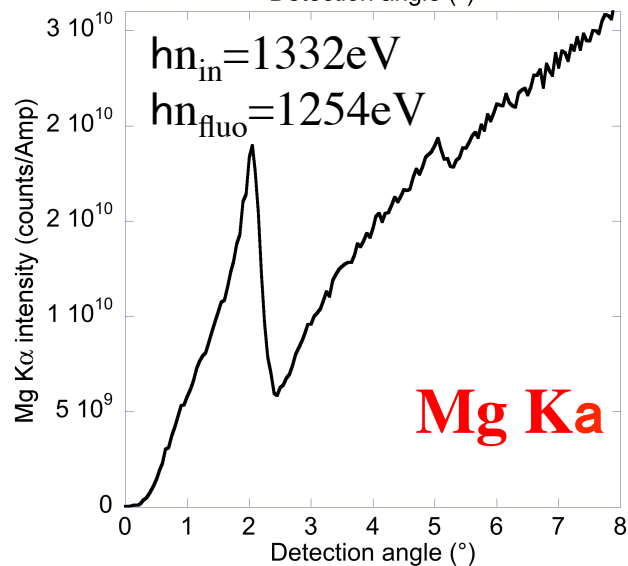
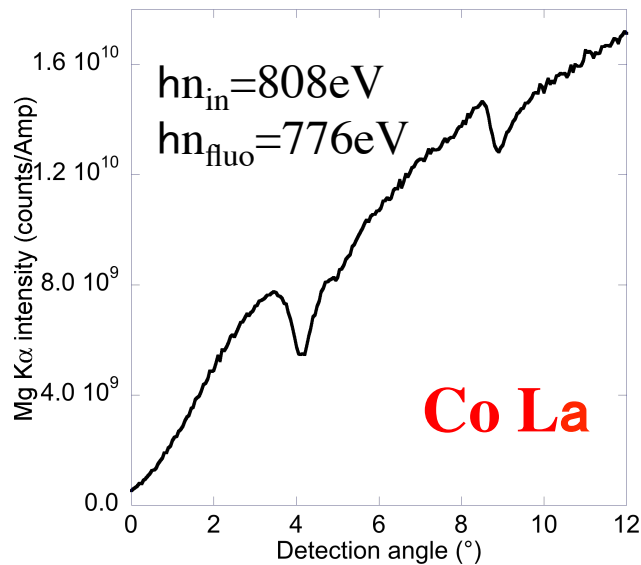
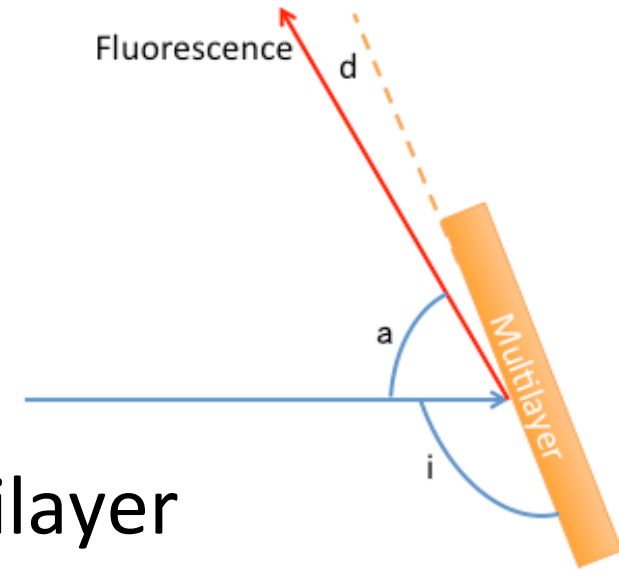
Si L_{2,3} (3sd – 2p) emission

M. Beye et al. Nature 12, 449 (2013)

First observation of the stimulated emission in a solid
with pumping by an X-FEL

Threshold: 10^{11} photons/shot

DFB laser

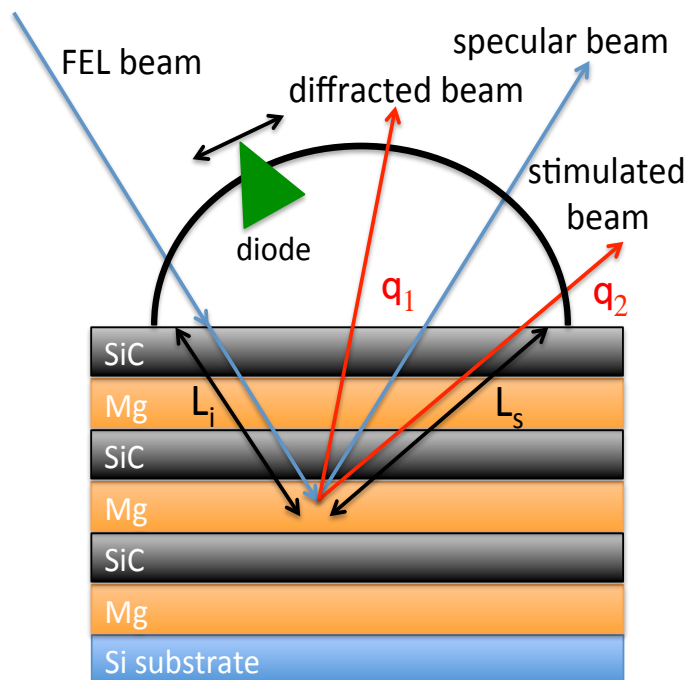


- Mg/Co multilayer
- Spontaneous emission
- Mg Ka and Co La fluorescence

Kossel effect =
**Diffraction of
spontaneous emission**

DFB laser

- Stimulated emission
Mg $L_{2,3}$ (3sd–2p) @ 49 eV



- FEL pump @ 57 eV

- Cavity

Mg/SiC periodic multilayer

- Detection angle, optimal for q_1

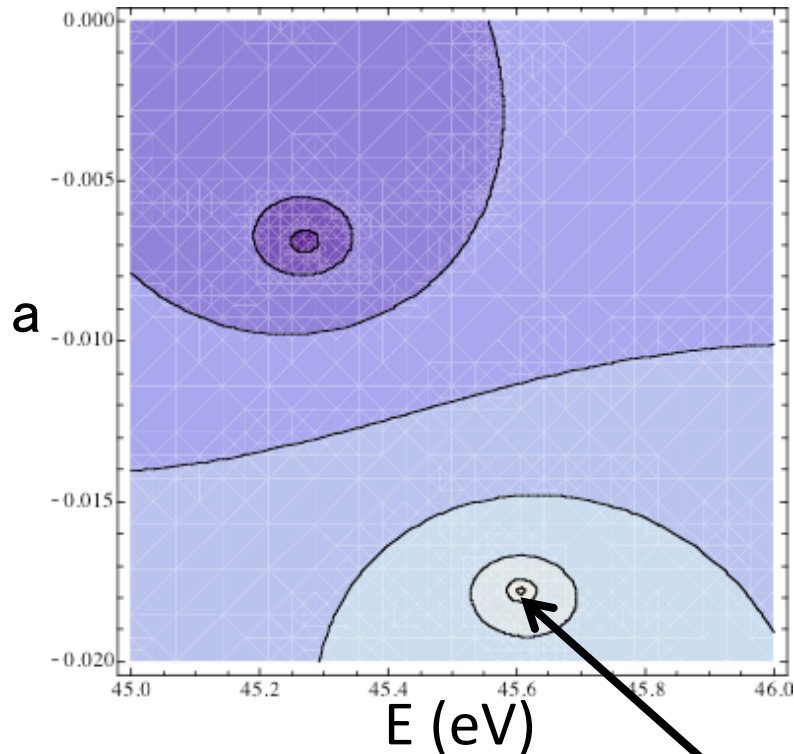
Stimulated emission @ 21°

(Beye *et al.* criterion)

DFB laser

Threshold for gain and lasing energy given by the relectivity poles of $R(E, a)$ curves (Yeh-Yariv criterion)

E : photon energy
 a : gain of active medium



Iso-reflectivity curves
in the E, a plane

Pole: $E_{\text{lasing}} = 45.6 \text{ eV}$

$a_{\text{threshold}} = 17.8 \cdot 10^{-3}$ or 78600 cm^{-1}

Conclusion

- Time dependence
 - + transient period conditioned by the extinction length
 - + reflectivity could be much lower than in the steady state
- DFB
 - + stimulated emission in a specific direction
 - + no spectral jitter
 - + mono-mode