



10828

## **Bridging the gap between particulate systems and continuum theory**

Stefan Luding, MSM, CTW, MESA+, UTwente, NL



VICI 2011-2014,...



soil, sand,  
powders,  
concrete,  
ceramics,  
cells, blood,  
...



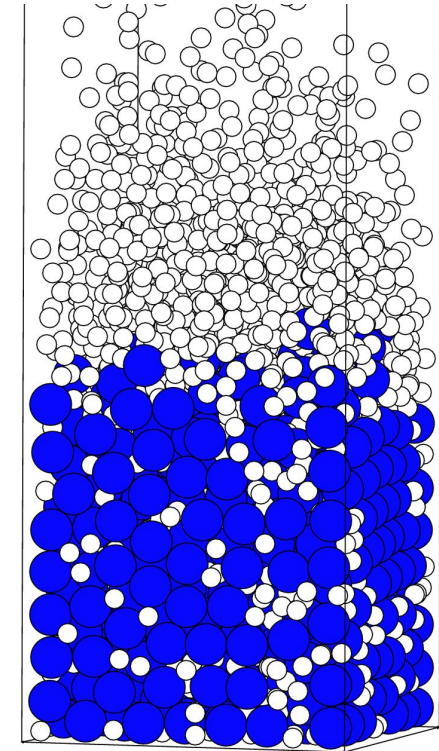
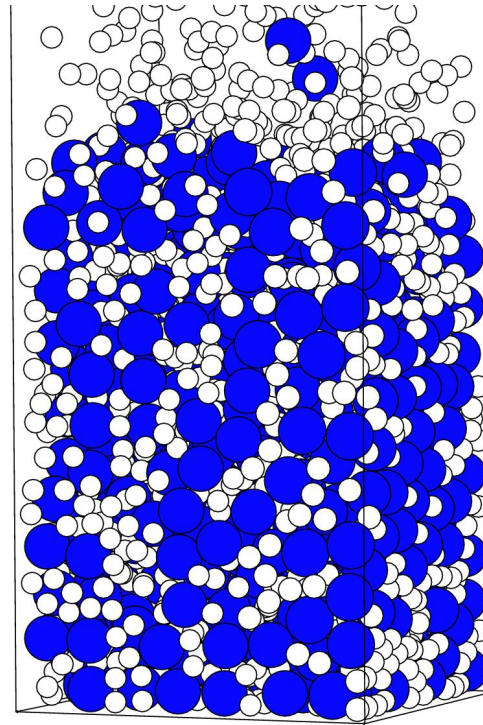
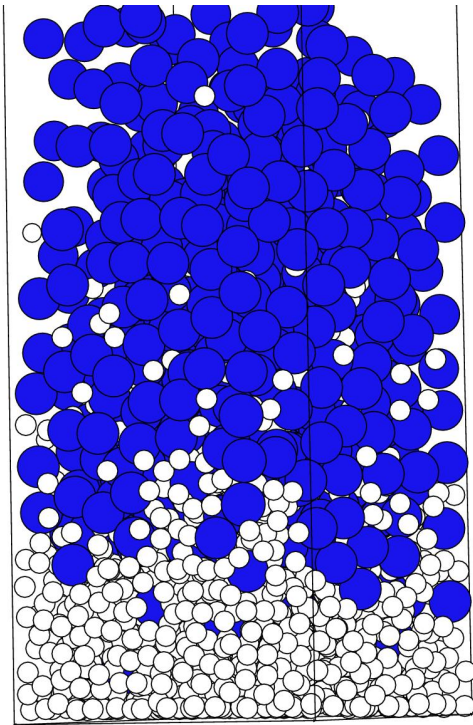
**particulate systems**

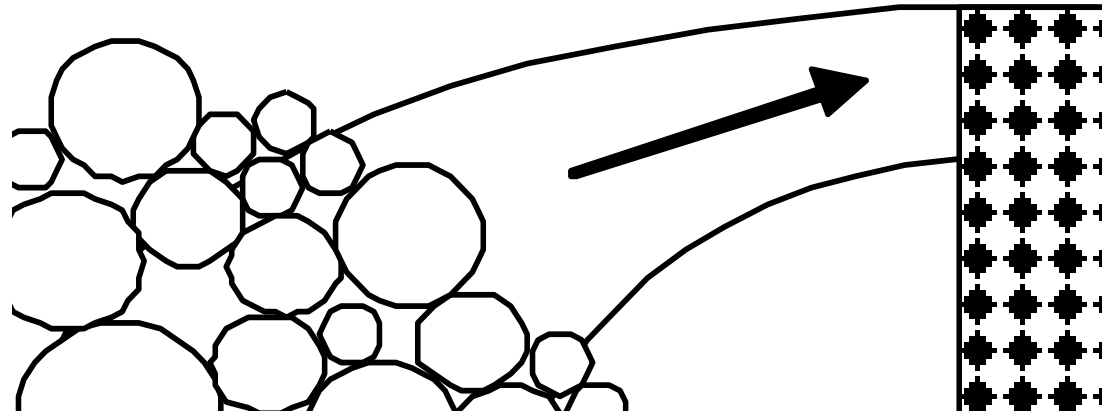
NWO STW VICI

msm

**Example:**

# **Segregation/Mixing**





Bridging the **gap** between  
particulate systems

from microscopic understanding  
and continuum theory  
towards macroscopic applications

# Why?

- Particle Methods (Micro-Details)
- Method: Micro-Macro Transition
- Continuum Theory (Applications)

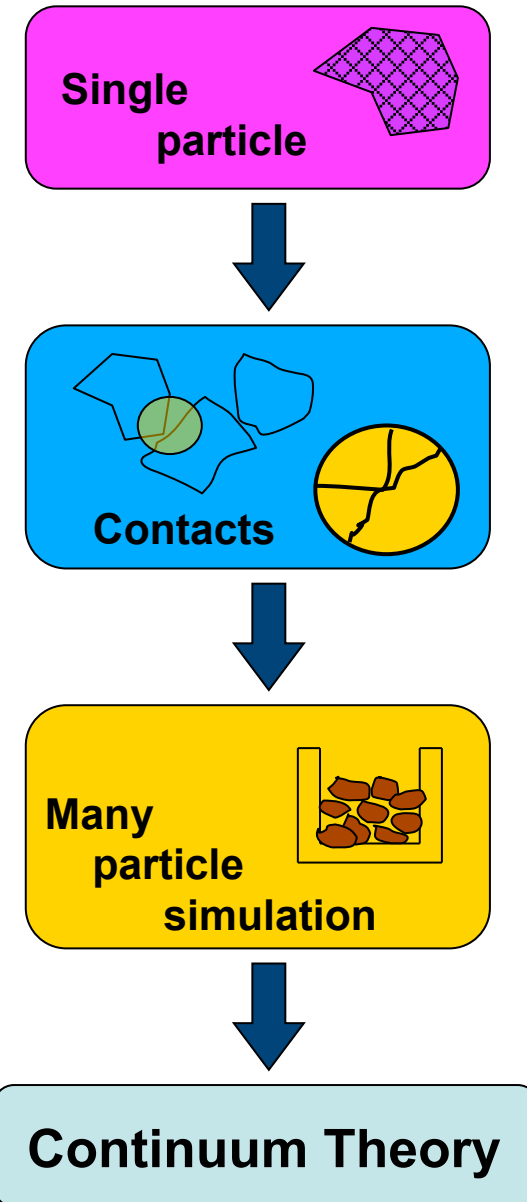
## Silo-collapse



**Continuum Theory**

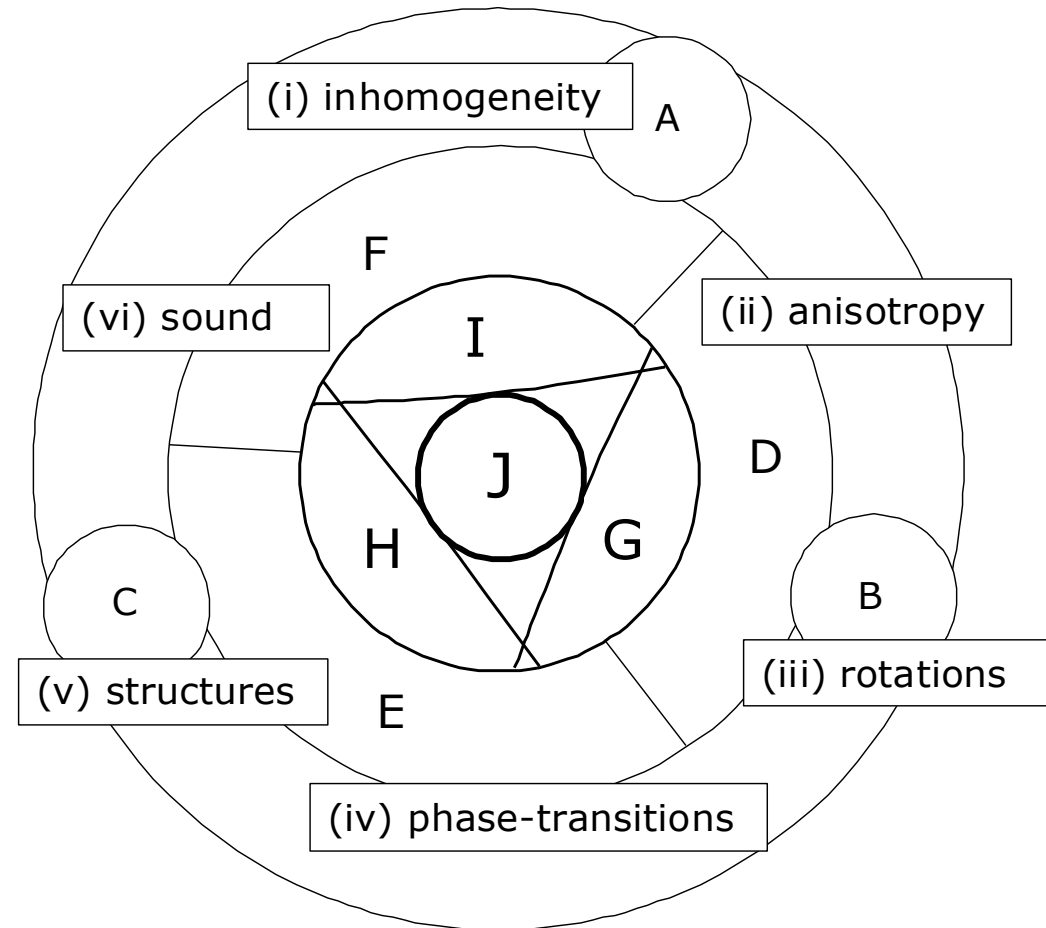
# Approach

- Particle Methods
- Micro-Macro Transition
- Towards Continuum Theory
- Applications



# Topics ...

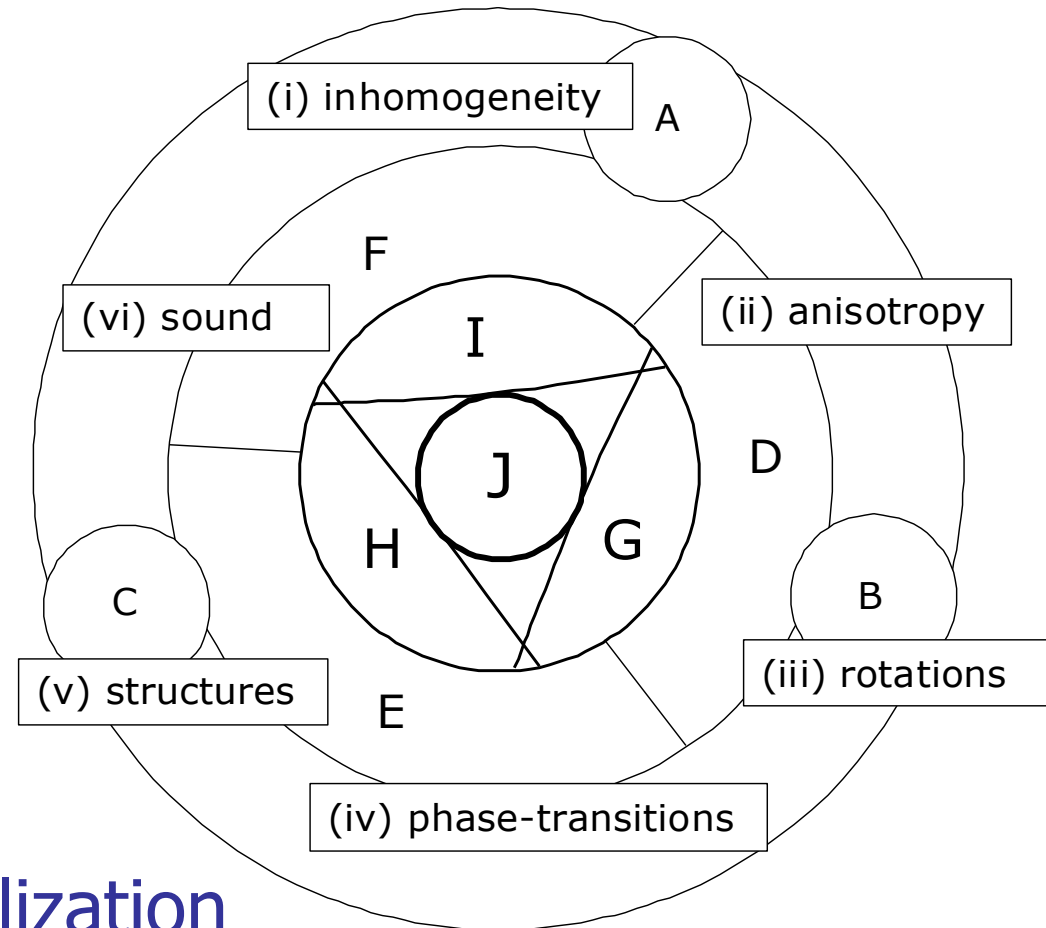
- inhomogeneity
- anisotropy
- rotations
- phase-transitions
- structures
- sound
- ...



# Topics ...

- inhomogeneity
- anisotropy
- rotations

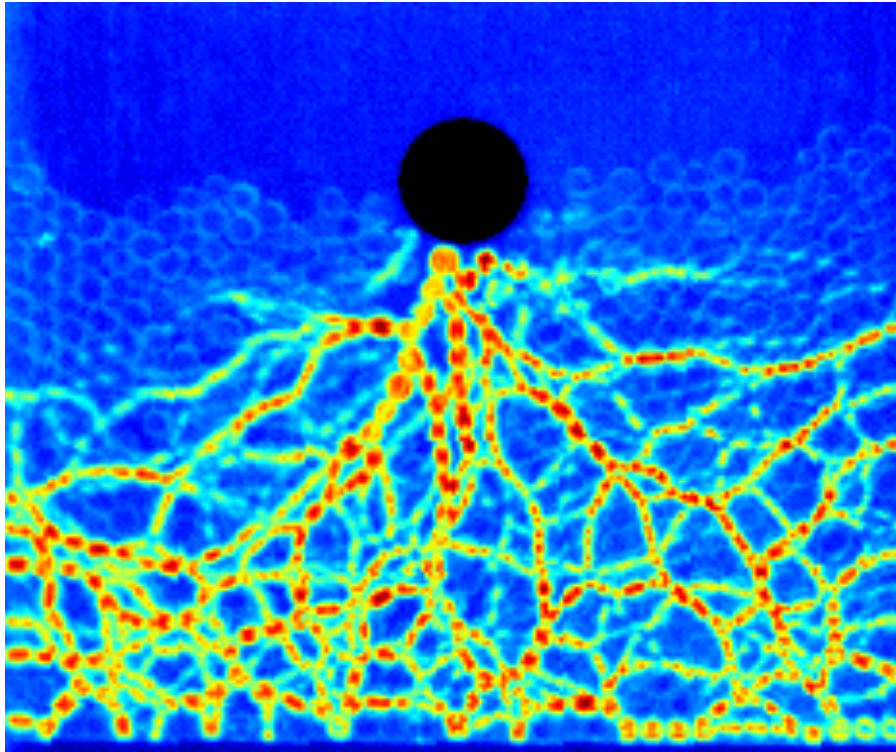
Example:  
Instability &  
Shear band Localization





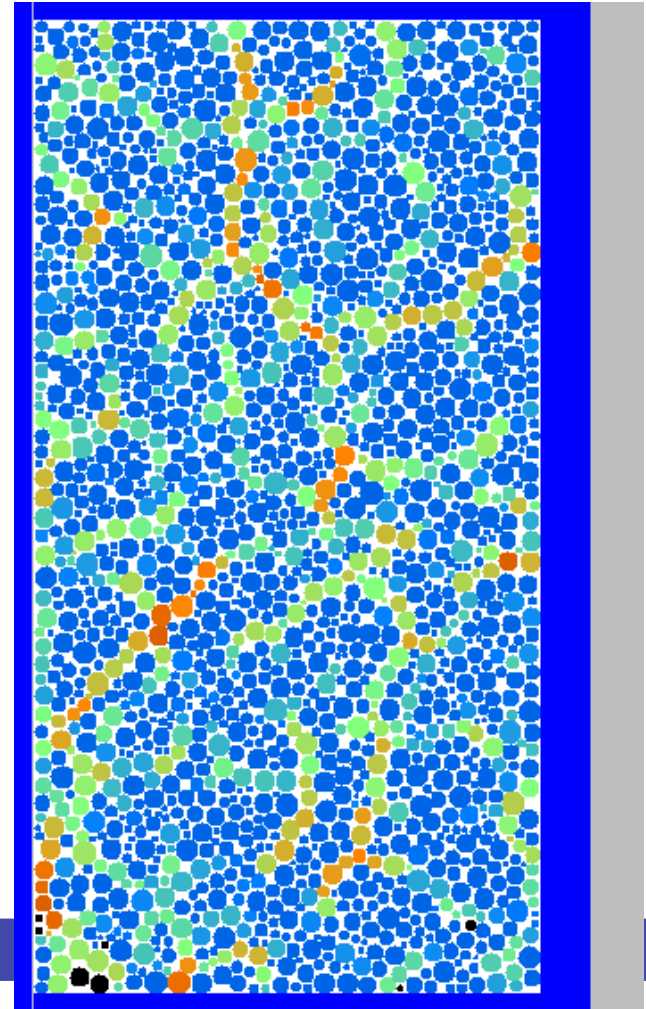
# Force-chains

## experiments - simulations



2D Exper. Behringer, Duke, USA

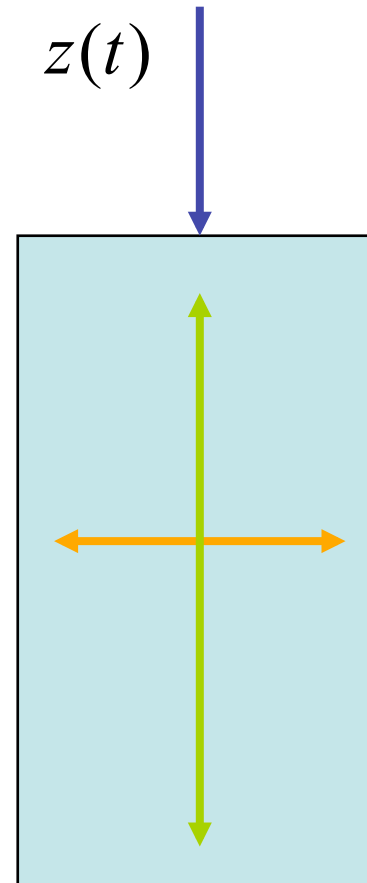
... 3D Exp. Sperl, DLR, Germany



# Biaxial box set-up

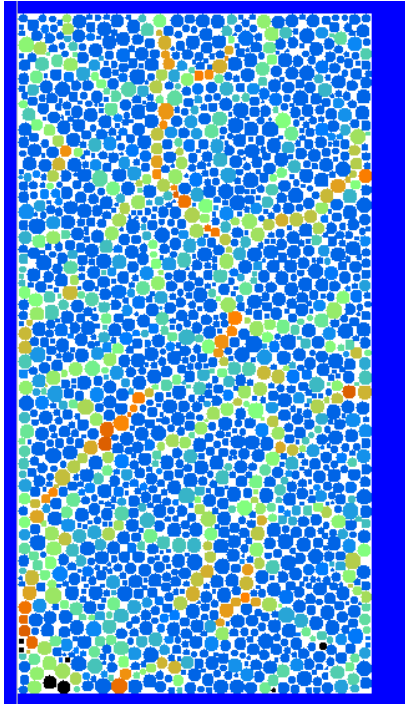
- Top wall: strain controlled
- Right wall: stress controlled

$$\sigma_{xx} = \text{const.} \longrightarrow$$

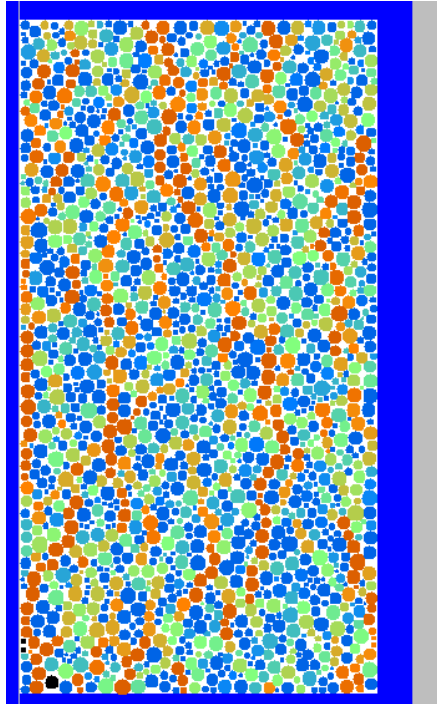


# Simulation results (closer look)

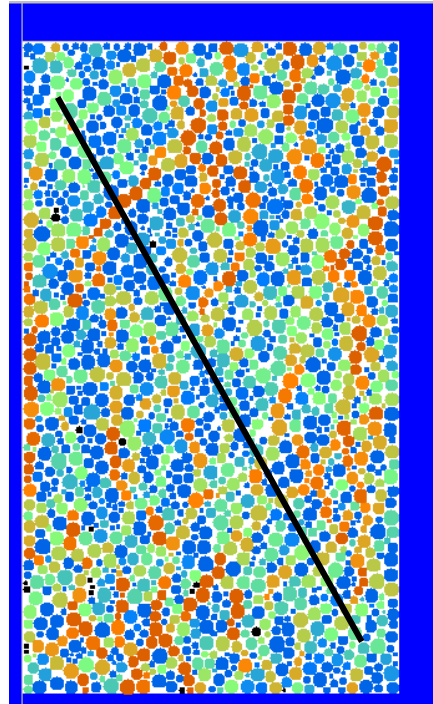
$\varepsilon_{zz}=0.0\%$



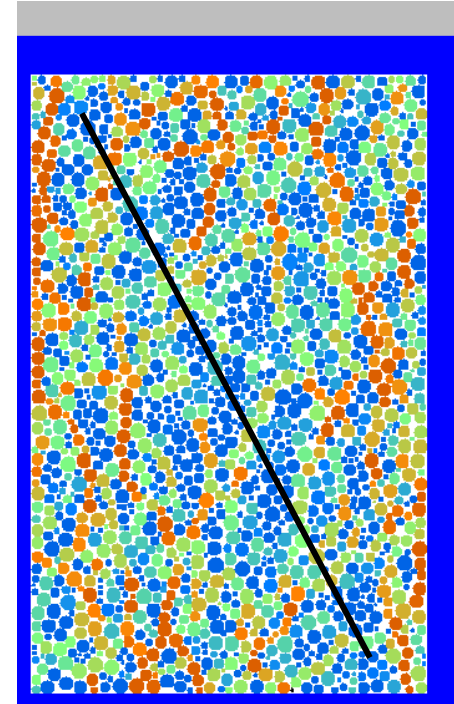
$\varepsilon_{zz}=1.1\%$



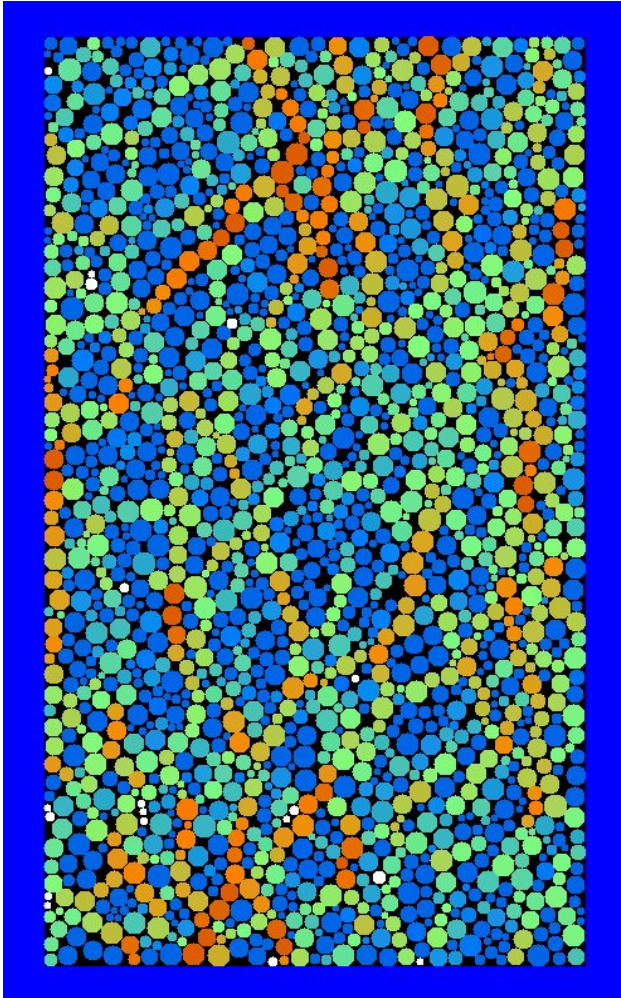
$\varepsilon_{zz}=4.2\%$



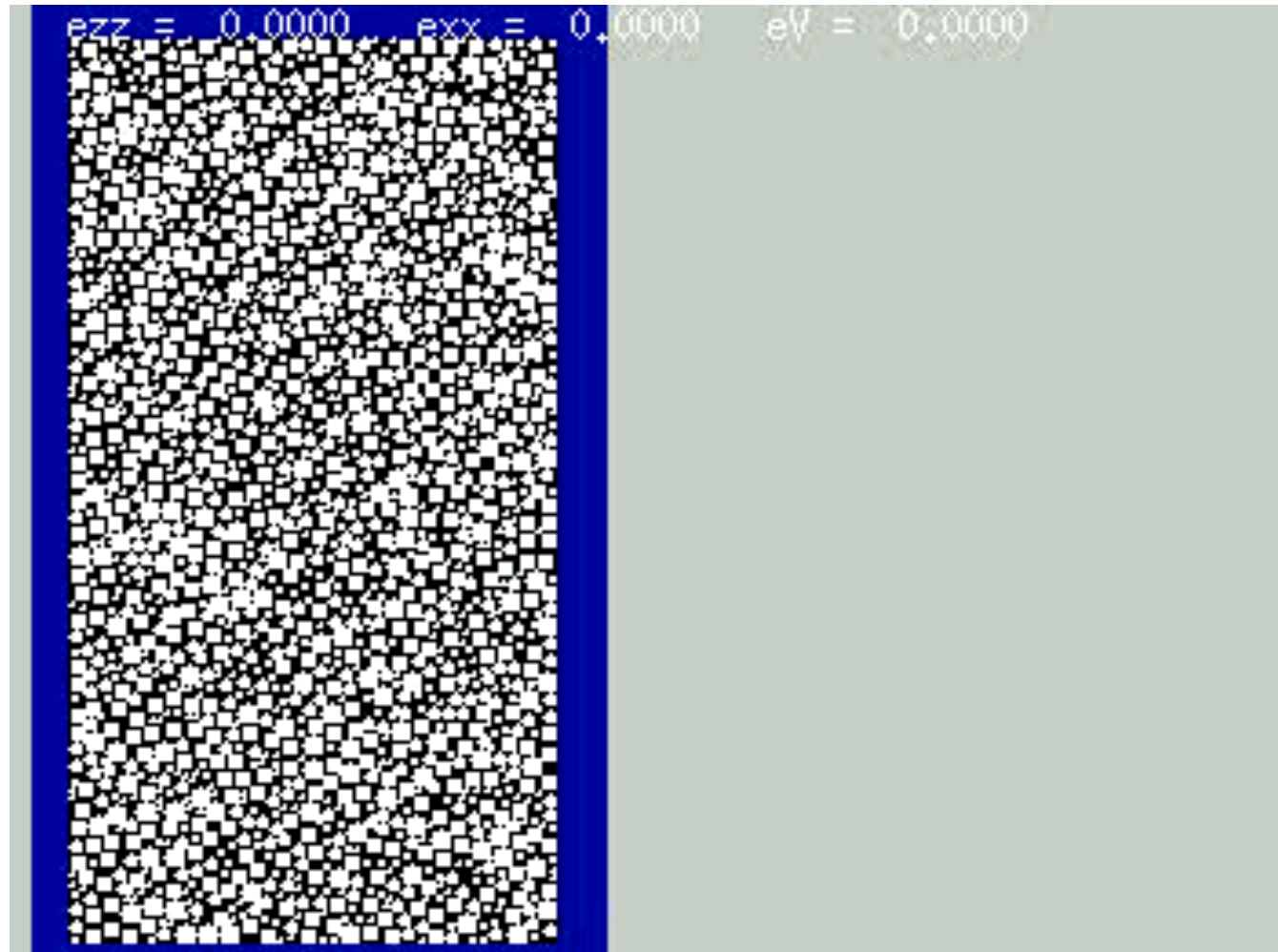
$\varepsilon_{zz}=9.1\%$



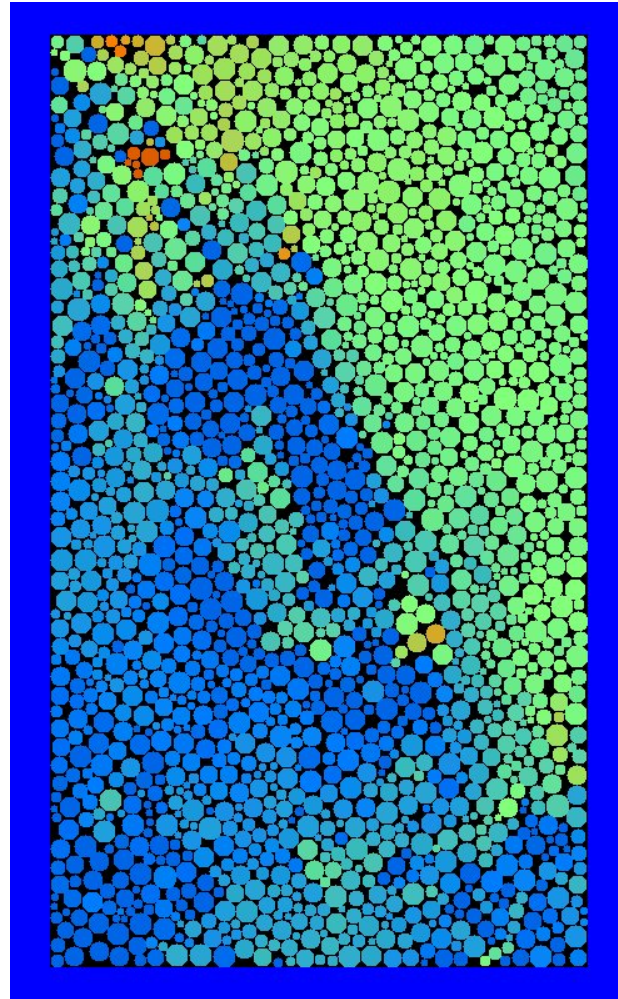
# Bi-axial box (stress chains)



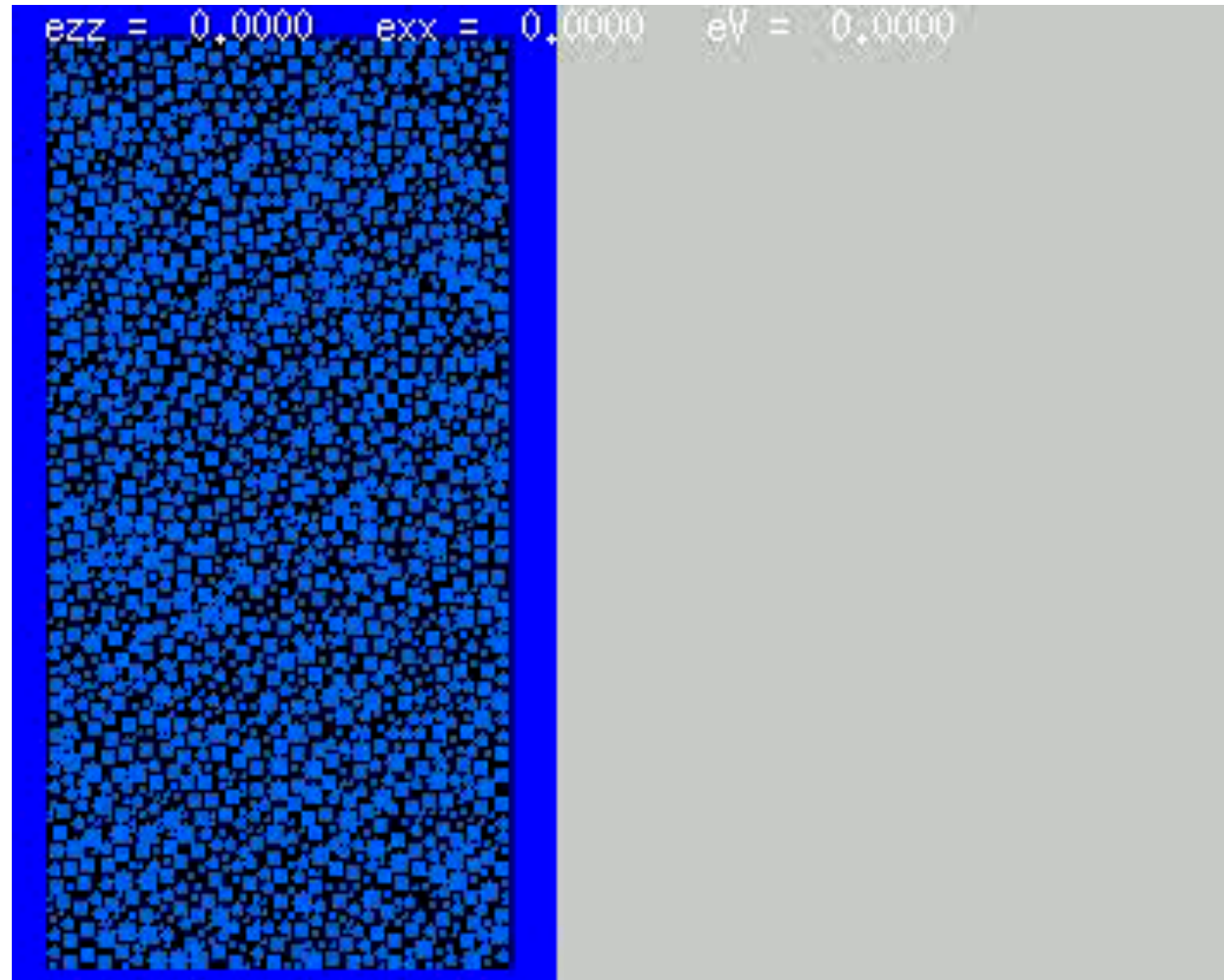
# Bi-axial box (stress chains)



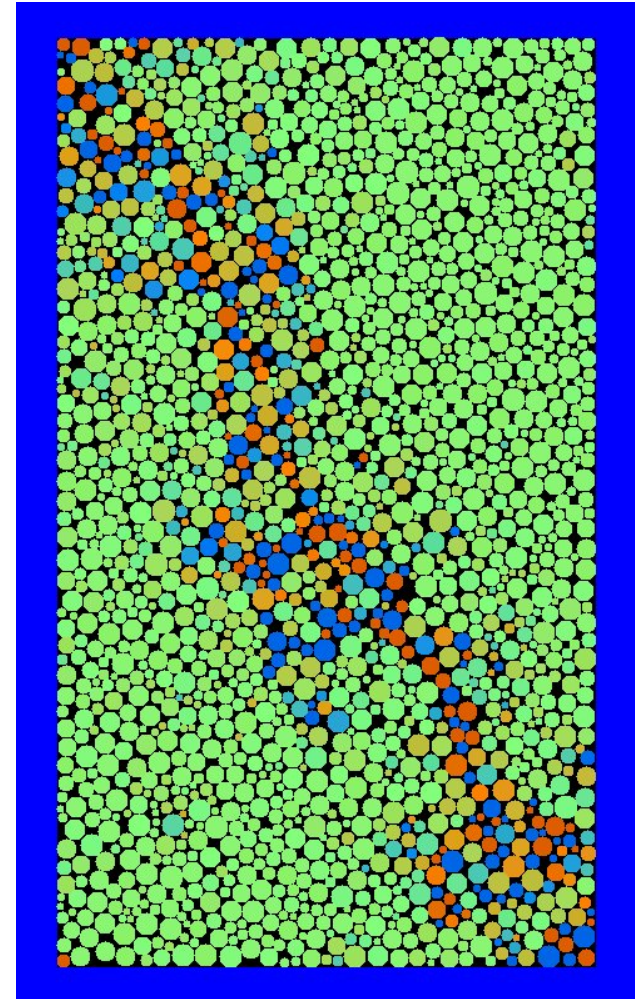
# Bi-axial box (kinetic energy)



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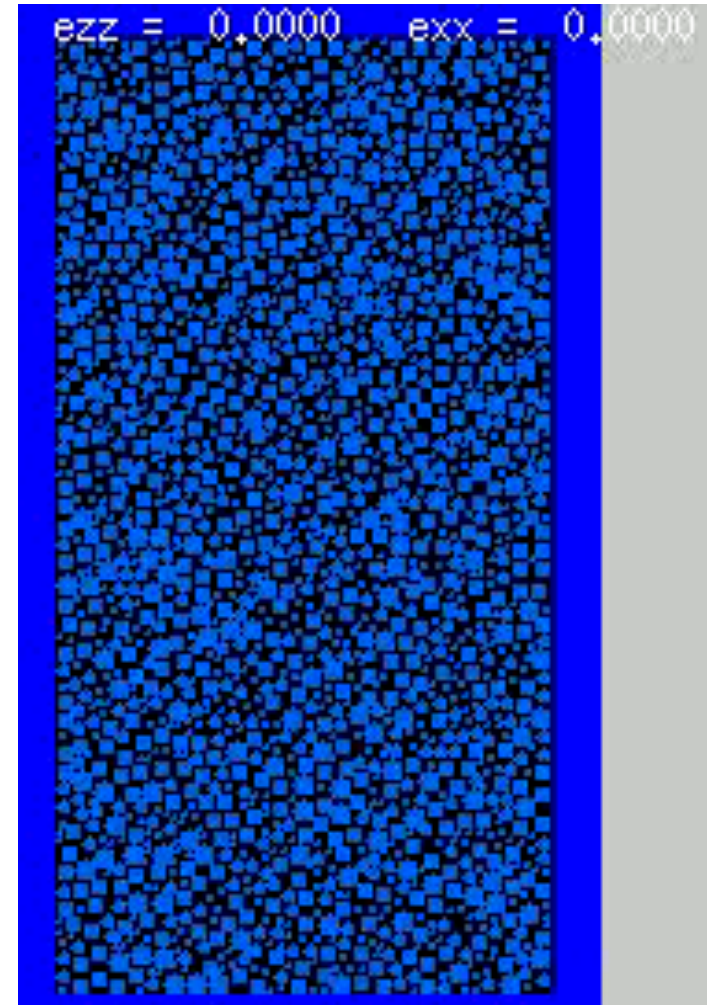


# Bi-axial box (rotations)

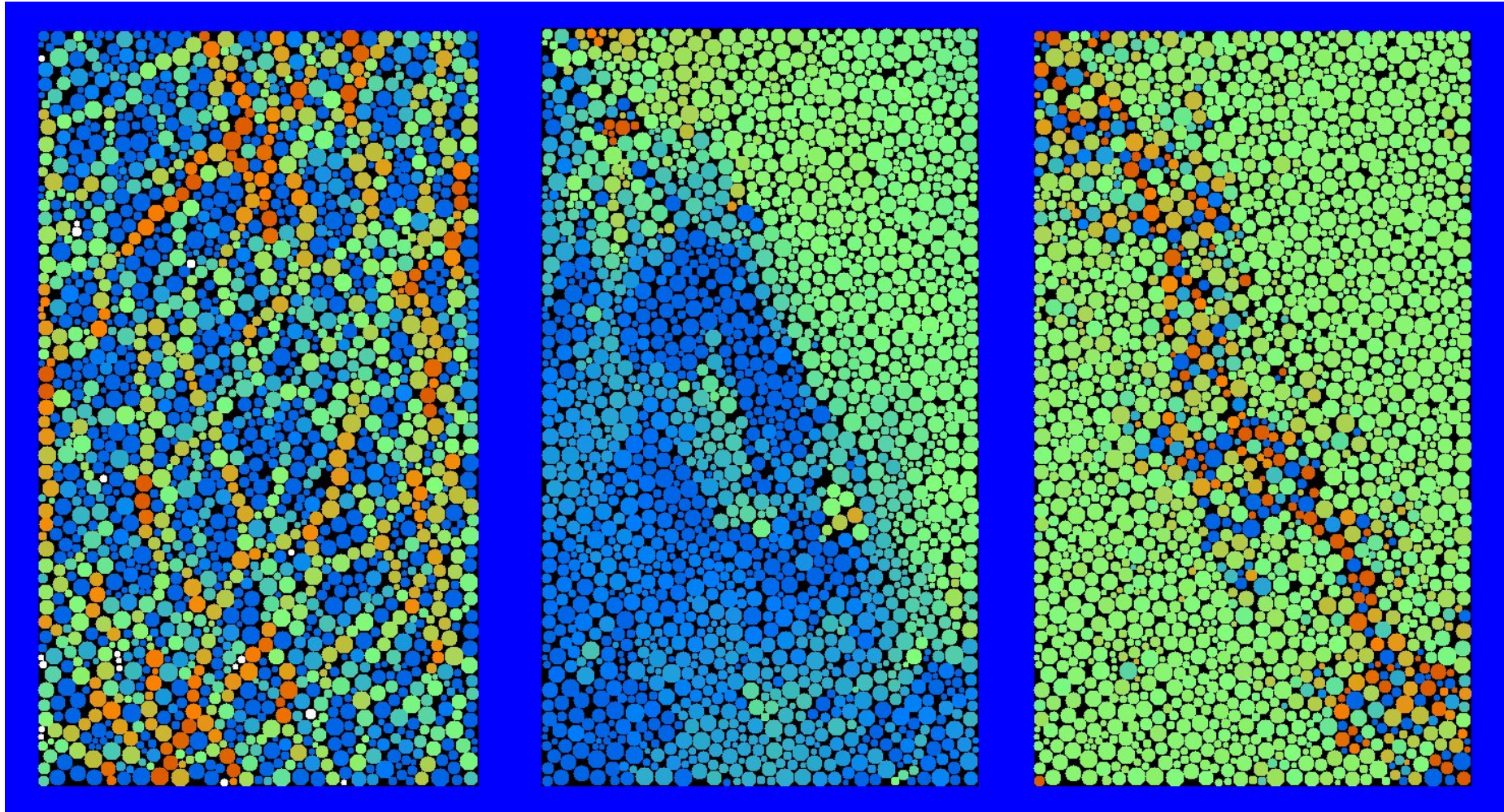




# Bi-axial box (rotations)



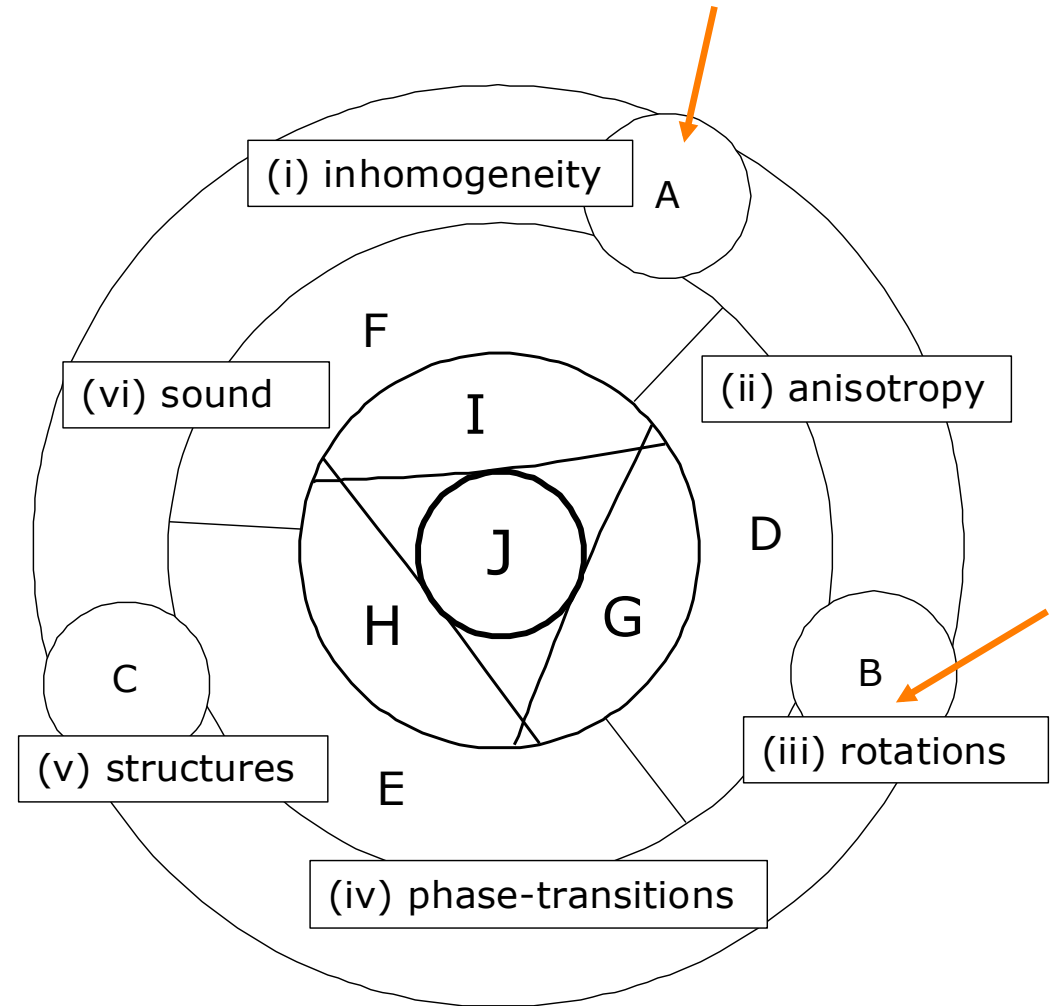
# Multiple micro-mechanisms



inhomogeneity & anisotropy, instabilities & structures, rotations

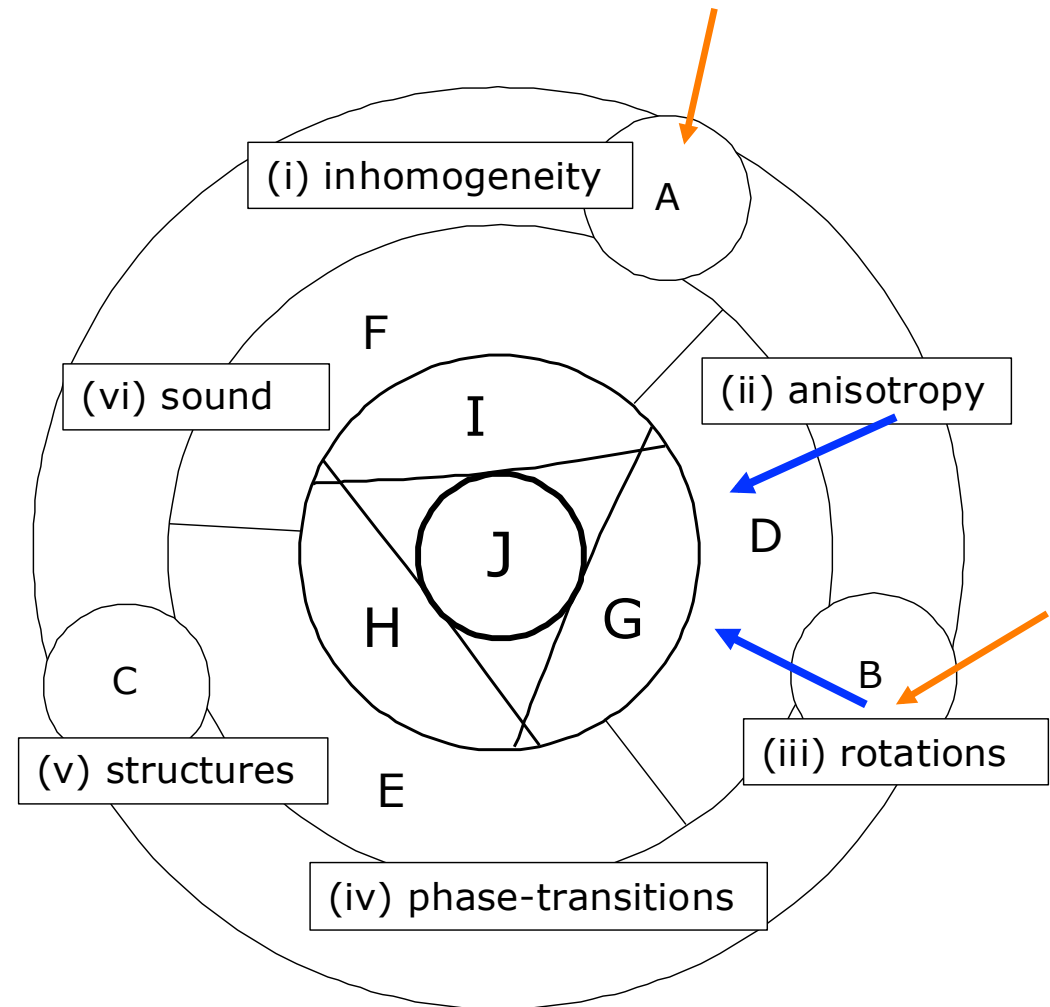
# How?

- inhomogeneity
- anisotropy
- rotations



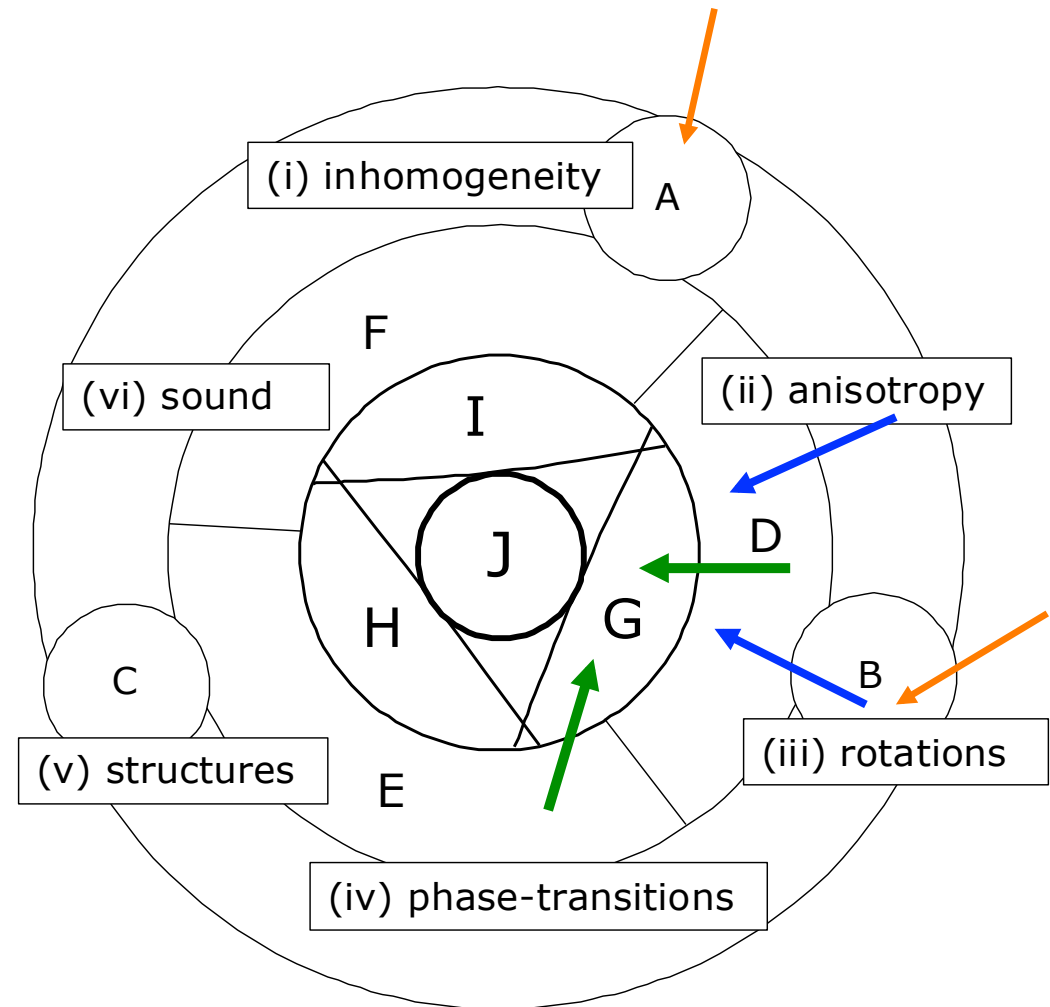
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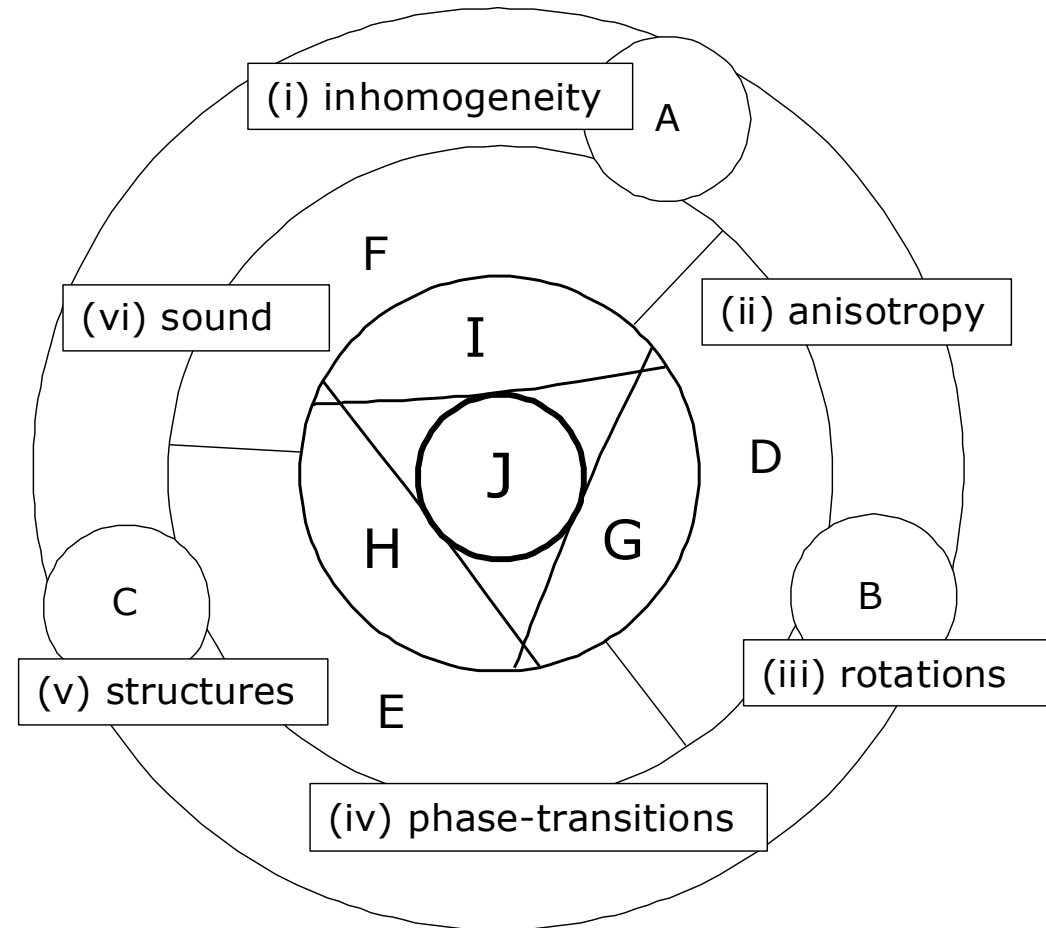
# How?

- inhomogeneity
- anisotropy
- rotations



# Themes worked on?

- inhomogeneity
- anisotropy
- rotations
- phase-transitions
- structures
- sound
- mixing
- ...



# Themes worked on?

- inhomogeneity, non-affine motion, master-pdf(force)
- **anisotropy continuum model**
- rotations (contact+particle => continuum)
- **phase-transitions (fluid-solid, jamming)**
- **structures (micro+macro, analysis => prediction)**
- **sound/waves**
- **mixing/polydispersity/multiscale**
- ...



# Overview – who and what?

- inhomogeneity (A. Singh, K. Saitoh, N. Rivas)
- anisotropy (T. Weinhart, D. Krijgsman, R. Hartkamp, A. Singh)
- rotations (A. Merkel, T. Weinhart, V. Magnanimo)
- phase-transitions/jamming: (N. Rivas, K. Saitoh, T. Weinhart, N. Kumar (PARDEM))
- structures (micro: A. Singh, macro: N. Rivas)
- sound (B. Lawney, A. Merkel, V. Magnanimo, MSc: L. de Mol, S. Emmerich, S. Sterl, ...)
- mixtures (N. Rivas, D. Krijgsman, T. Weinhart, A. Thornton, D. Tunuguntla (STW), ...)

- ...




# How?

- Particle methods numerics and validation
- Micro-macro methods, combining statistical physics and mechanics
- Fluid and Solid Mechanics
- Continuum Theory for Applications



# Collaborations?

- Particle methods (MSM) validation (PARDEM)
  - Micro-macro methods (FOM, STW)
  - Fluid (JMBC) and Solid Mechanics (EM)
    - ... Continuum Theory (UT-CTW, ...)
  - Statistical & Exp. Physics (DLR, Duisburg, ETHZ)
  - Mechanical and Chemical Engineering (e.g. BASF)
  - Food (Nestle) & Pharma Industry (BI-Mainz)
- 

# Applications:

- sound-propagation in soils, disordered modern/  
bio-materials for **non-invasive tests**
- clustering-/structure-formation in aerosols  
and chemical engineering **processes**
- prediction of **instabilities and failure**  
in soils and engineering structures
- **material properties and behavior** in  
micro-/nano (fluid&solid) systems



# Applications:

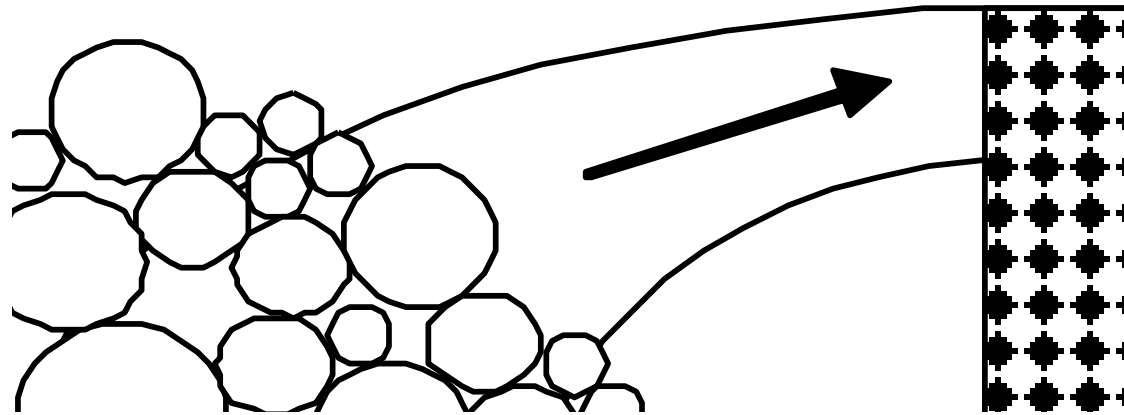
- sound-propagation in soils, disordered modern/bio materials for **non-invasive tests**
- clustering-/structure-formation in aerosols and chemical engineering **processes**
- prediction of **instabilities and failure** in soils and engineering structures
- **material properties and behavior** in micro-/nano (fluid&solid) systems

**Impact:** Avoid energy-loss, improve safety, improve durability, reduce costs



# Program:

- 13:30-13:35 S. Luding, Opening: *"Bridging the gap between discrete and continuum models"*,
- 13:35-13:50 K. Saitoh: *"Stochastic approach to the PDFs of forces"*,
- 13:50-14:05 N. Rivas: *"Particle size scaling in vertically vibrated granular media"*,
- 14:05-14:20 D. Krijgsman: *"Optimal parameters for contact detection using a hierarchical grid data structure"*
- 14:20-14:35 T. Weinhart: *"From discrete particles to continuum fields in mixtures"*
- 14:35-14:50 A. Singh: *"Does gravity have an effect on the slow shear rheology of granular material?"*,
- 14:50-16:00 Coffee break -> UC Meeting**
- 16:00-17:00 M. Sperl: *"The Glass Transition in Granular Matter"*
- 17:00-18:00 L. Silbert: *"Static and Dynamic Perturbations in Granular Materials"*,



Bridging the **gap** between  
particulate systems

from microscopic understanding  
and continuum theory  
towards macroscopic applications

NWO STW VICI

*msm*