Misfit strain accommodation in epitaxial $ABO_3$ perovskites: Lattice rotations and lattice modulations

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We present a study of the lattice response to the compressive and tensile biaxial stress in La$_{0.67}$Sr$_{0.33}$MnO$_3$ (LSMO) and SrRuO$_3$ (SRO) thin films grown on a variety of single-crystal substrates: SrTiO$_3$, DyScO$_3$, NdGaO$_3$, and (La,Sr)(Al,Ta)O$_3$. The results show that, in thin films under misfit strain, both SRO and LSMO lattices, which in bulk form have orthorhombic (SRO) and rhombohedral (LSMO) structures, assume unit cells that are monoclinic under compressive stress and tetragonal under tensile stress. The applied stress effectively modifies the BO$_6$ octahedra rotations, whose degree and direction can be controlled by the magnitude and sign of the misfit strain. Such lattice distortions change the B-O-B bond angles and therefore are expected to affect magnetic and electronic properties of the ABO$_3$ perovskites.

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I. INTRODUCTION

The presence of strong electron-lattice correlations in transition-metal oxides with ABO$_3$ perovskite-type structures imply that the lattice distortions play an important role on the physical properties in these materials, such as colossal magnetoresistance, ferroelectricity, superconductivity, charge density waves, and superconductivity. BO$_6$ octahedra deformations usually are present through a Jahn-Teller distortion (e.g., in LaMnO$_3$) or cation displacement (ferroelectricity in PbTiO$_3$, BaTiO$_3$). Another group of ABO$_3$ perovskite-type materials possesses almost rigid octahedral, and strain accommodation can be mainly achieved through octahedral rotations and tilts.

The general formula for a perovskite unit cell can be written as ABO$_3$, where atom A sits in the center of the unit cell with coordinates (1/2 1/2 1/2) and atom B is located at the unit cell corners (0 0 0). The oxygen is then placed between B atoms at (1/2 0 0) positions. In such an arrangement, the B cation is surrounded by six oxygens, forming a corner-sharing BO$_6$ octahedra. The simplest perovskite structure is cubic, such as of SrTiO$_3$ (STO) at room temperature, and belongs to space group $Pm-3m$. By substituting A and B cations, a large number of perovskite-type oxides with different properties can be obtained. Generally, the substitutions in such oxides must obey a rule imposed by the ionic radii of the cations, which is known as the Goldschmidt tolerance factor:

$$ t = \frac{R_A + R_O}{\sqrt{2(R_B + R_O)}} $$

where $R_A$, $R_B$, and $R_O$ are ionic radii of A and B cations and oxygen, respectively. Common perovskite-type compounds usually exhibit a tolerance factor of 1.05 $> t > 0.78$. The variation in cation ionic radii induces small deformations or rotations of BO$_6$ octahedra and thus lowers the unit-cell symmetry from cubic to tetragonal, orthorhombic, rhombohedral, monoclinic, or triclinic.

The changes in the unit-cell symmetry resulting from different octahedral rotations have been systematized by Glazer and later expanded by Woodward. Octahedral rotations in the perovskite-type unit cell can be described as a combination of rotations about three symmetry axes of the pseudocubic unit cell: [100], [010], and [001]. The relative magnitudes of the tilts are denoted by letters a, b, and c, e.g., $aab$ means equal rotations around [100], and [010] axes and...
and a different tilt around the [001]_c axis. Two adjacent octahedra around one of the (100)_c axes can either rotate in phase or out of phase, which is indicated by the + or - sign, respectively. No rotation is indicated by the “0” sign. Two of the simplest systems that are possible in perovskite materials with rigid structures: PrNiO₃, LaNiO₃, CaRuO₃, etc. which in bulk form exhibit orthorhombic or rhombohedral behavior is common in other strained perovskite thin films, e.g. SrO, which in epitaxial La₀.₅Sr₀.₅MgO₃ (Ref. 17) and SrRuO₃ (Ref. 18) films were grown by pulsed laser deposition at 800 (700) °C from stoichiometric targets in an oxygen background pressure of 0.16–0.27 mbar (0.4 mbar, mixed 50% O₂ + 50% Ar). A KrF excimer laser (λ = 248 nm) was used with a fluence of 2 J/cm² and a pulse repetition rate of 5 (4) Hz. The target-to-substrate distance was fixed at 5 cm. After deposition, the films were cooled down to room temperature at a rate of 10°C/min in a 1-bar pure oxygen atmosphere. Atomic force microscopy measurements showed smooth surfaces with unit-cell high steps.

X-ray diffraction (XRD) measurements were performed using a PANalytical X’Pert materials research diffractometer in high- and medium-resolution modes at the Stanford Nanofacilitation Laboratory, Stanford University, as well as at the beamline 7-2 of the Stanford Synchrotron Radiation Laboratory at SLAC, Stanford University. High-temperature measurements were performed using an Anton-Paar hot stage. Mn K-edge extended x-ray absorption fine structure (EXAFS) measurements were performed in the fluorescence mode at the beamline 4-2 of the Stanford Synchrotron Radiation Laboratory at SLAC, Stanford University. EXAFS data were acquired at room temperature in two orientations: electrical vector of the synchrotron light at 80° from the sample surface normal (in-plane orientation) and with the electrical vector at 10° from the sample surface normal (out-of-plane orientation).

III. RESULTS AND DISCUSSIONS

A. Unit-cell structures of bulk SRO and LSMO

Room-temperature bulk SrRuO₃ possesses an orthorhombic crystal structure with space group Pbnm (No. 62) and lattice constants aᵦ = 5.5670 Å, bᵦ = 5.5304 Å, and cᵦ = 7.8446 Å, and it is isostructural with a GdFeO₃ perovskite. The orthorhombic unit cell is a result of cooperative BO₆ octahedra tilts and rotations induced by the mismatch between the A-O and √2(B-O) bond lengths. According to Glazer notation, the orthorhombic SRO structure can be described by the tilt system #10: a⁺b⁻c⁻, which defines the in-phase octahedral rotations about the pseudocubic [100], axis and mutually equivalent out-of-phase rotations about the [010], and [001]ₜ axes. The SRO orthorhombic unit cell with a ≠ b ≠ c and α = β = γ = 90° can be related to the tilted pseudocubic unit cell through the following relationships (see Fig. 2):

\[ a_c = \frac{c_o}{2}, \]

\[ b_c = \frac{\sqrt{a_o^2 + b_o^2 - 2a_o b_o \cos \gamma_o}}{2}, \]

\[ c_c = \frac{\sqrt{a_o^2 + b_o^2 - 2b_o^2}}{2}, \]

\[ a_c = \cos \left( \frac{b_o^2 + c_o^2 - a_o^2}{2b_o c_o} \right), \]

where \( a_o, b_o, c_o \) are the lattice constants of the orthorhombic SRO unit cell, and \( a_c, b_c, c_c \) are the lattice constants of the tilted pseudocubic unit cell.
FIG. 2. (Color online) The relationship between distorted orthorhombic (monoclinic) and pseudocubic unit cells: (a) Unit cell under compressive stress and (b) unit cell under tensile stress.

where \( a_e, b_o, c_o, \alpha_o, \beta_o, \gamma_o \) are pseudocubic (distorted cubic) unit-cell lengths and tilt angle and the distorted orthorhombic unit-cell lengths and tilt angle, respectively. Sometimes in the literature the SrRuO\(_3\) unit cell is described by using an approximate pseudocubic unit cell:

\[
a_e \approx \frac{a_o}{\sqrt{2}}, \quad b_o \approx \frac{c_o}{\sqrt{2}}, \quad \gamma_o \approx \frac{\alpha_o}{2}.
\]  

(3)

Bulk \( \text{La}_{0.67}\text{Sr}_{0.33}\text{MnO}_3 \) (LSMO) possesses a rhombohedral unit cell with space group \( \text{R}-3c \) (No. 167) and lattice constants \( a_o = 5.471 \, \text{Å} \) and \( \alpha_o = 60.43^\circ \). In this unit cell octahedra rotations are described by Glazer’s tilt system #14: \( a^\prime \cdot a^\prime \cdot a^\prime \), which consists of equivalent out-of-phase rotations about the \( \langle 100 \rangle \) cubic axes. The rhombohedral unit cell can be represented as a tilted fcc cubic cell through the following equations:

\[
a_f = \frac{\sqrt{2} a_o}{1 + \cos \alpha_f},
\]

\[
\alpha_f = \arccos \left( \frac{1 - 2 \cos \alpha_e}{2 \cos \alpha_e - 3} \right),
\]

(4)

where \( a_f, \alpha_f, \alpha_e, \) and \( \alpha_e \) are the unit-cell lengths and angles of the tilted fcc cubic and rhombohedral unit cells, respectively. The approximate tilted pseudocubic unit-cell parameter in this case can be approximated as \( a_e \approx a_f/2 \).

B. Unit-cell structures of \( \text{ABO}_3 \) perovskites under tensile and compressive stress

Thin films that are coherently grown on single-crystal substrates undergo a change in the lattice parameters owing to a mismatch between the unit cells of the growing layer and the underlying substrate. According to Frank and van der Merwe, the lattice mismatch is defined as

\[
m = (a_i - a_s)/a_s,
\]

where \( a_i \) and \( a_s \) are the unstrained layer and substrate in-plane lattice constants, respectively. Let us initially describe SRO and LSMO thin-film unit cells under compressive and tensile stresses by using a distorted orthorhombic (monoclinic) unit cell with the lattice parameters \( a_o, b_o, c_o, \alpha_o, \beta_o, \) and \( \gamma_o \), where \( a_o = b_o = 90^\circ \), as shown in Fig. 2. Such a description is perfectly valid for SRO if \( \gamma_o = 90^\circ \). The LSMO unit cell also can be successfully described as a monoclinic unit cell, as has been reported elsewhere. The orientation of such a unit cell on (001)-oriented cubic and (110)-oriented orthorhombic substrates is shown in Figs. 3(a) and 3(b), respectively. In this study we used four different substrates: SrTiO\(_3\) (STO), NdGaO\(_3\) (NGO), DyScO\(_3\) (DSO), and (LaAlO\(_3\))\(_{0.33}\)–(Sr\(_2\)AlTaO\(_6\))\(_{0.7}\) (LSAT). The relationship between pseudocubic lattice parameters of the substrates and thin films is illustrated in Fig. 3(c).

In order to determine the unit-cell parameters of strained SRO and LSMO films, we used high-resolution XRD. Reciprocal lattice maps (RLM) taken at room temperature using symmetrical and asymmetrical reflections confirm that the SRO and LSMO layers were grown in a fully coherent fashion with respect to the underlying substrate. As an example, RLMs around the (260), (444), (620), and (44-4) reflections of LSMO films under compressive and tensile stresses are shown in Fig. 4. Epitaxial SRO thin films exhibit identical behavior. The difference in (260) and (620) atomic plane spacings shown in Fig. 4(a) represents a difference in the \( a_o \) and \( b_o \) film lattice parameters. For thin films under tensile stress, (620) and (260) reflections [see Fig. 4(b)] show identical positions indicating that \( a_o = b_o \). The sizes and shapes of the LSMO and SRO thin-film unit cells were determined by refining unit-cell parameters using six \((hkl)\) reflections: (220), (440), (260), (620), (444), and (44-4). The refined lattice parameters and the calculated strains are listed in Table I. As can be seen from Table I and Fig. 2, films under compressive stress possess a unit cell, with \( a_o < b_o, \alpha_o = \beta_o = 90^\circ \), and \( \gamma_o < 90^\circ \), while films under tensile stress exhibit a unit cell with \( a_o = b_o, \alpha_o = \beta_o = 90^\circ \), and \( \gamma_o > 90^\circ \).

As the stress changes from compressive to tensile, the \( \text{ABO}_3 \) unit cell accommodates that stress differently along perpendicular in-plane directions. Along the [001] direction...
TABLE I. Refined lattice parameters of SrRuO$_3$ and La$_{0.67}$Sr$_{0.33}$MnO$_3$ thin films grown on different substrates. Bulk values of the orthorhombic SRO and LSMO materials together with the substrate lattice parameters are also shown.

<table>
<thead>
<tr>
<th>Substrate and bulk SRO and LSMO</th>
<th>Strained layer</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>a (Å)</td>
</tr>
<tr>
<td>NdGaO$_3$ (Ref. 25)</td>
<td>5.428</td>
</tr>
<tr>
<td>LSAT (This work)</td>
<td>5.476</td>
</tr>
<tr>
<td>SrTiO$_3$</td>
<td>5.405</td>
</tr>
<tr>
<td>DyScO$_3$ (Ref. 26)</td>
<td>5.442</td>
</tr>
<tr>
<td>LSMO (O) (Ref. 27)</td>
<td>5.488</td>
</tr>
<tr>
<td>SRO (O) (Ref. 19)</td>
<td>5.530</td>
</tr>
</tbody>
</table>

Strain (%): Along ab = -0.80, Along c = -0.60, Along ab = -0.55, Along c = 0.29, Along ab = 1.39, Along c = 1.48, Along ab = -0.44, Along c = -0.45, Along ab = 0.64, Along c = 0.74

Glazer tilt system

FIG. 4. (Color online) Reciprocal lattice maps around (620), (260), and (444) Bragg reflections of La$_{0.67}$Sr$_{0.33}$MnO$_3$ films grown (a) on a NdGaO$_3$(110) substrate under compressive stress and (b) on a SrTiO$_3$(001) substrate under tensile stress. Here we used $Q_{\perp} = 4\pi \sin(\theta/\lambda)$, where $\theta$ is the Bragg angle and $\lambda = 1.540598$ Å.
along the [1-10]_o direction is achieved by varying only the \( \gamma_c \) angle. Owing to the \( b_o/a_o \) axis collapse, the orthorhombicity (\( b_o/a_o \) ratio) of LSMO and SRO films also abruptly drops to unity as the film strain changes from compressive to tensile, as shown in Fig. 5(b). The volume of the thin-film unit cells within the measured strain range increases linearly with strain as predicted by Zayak \textit{et al.} \cite{zayak2005} and is shown in Fig. 5(c). The absolute volume values of the SRO films are somewhat higher than those calculated, probably owing to the underestimation of the lattice constant values in the local spin-density approximation.\cite{zayak2005}

C. \( \text{BO}_6 \) octahedra rotations under compressive stress

The change from \( a_o < b_o \) for compressive stress to \( a_o = b_o \) for the tensile stress unequivocally indicates a change in the \( \text{BO}_6 \) octahedra rotation pattern. We will use Glazer notations to describe the \( \text{BO}_6 \) octahedra rotations and corresponding lattice symmetries of thin epitaxial SRO and LSMO films. Because the layers are coherently strained to the substrate, the film’s pseudocubic in-plane lattice constants should match the ones of the substrate. Assuming that the substrate’s in-plane lattice parameters are equal (\( a_s = b_s \)), for compressively strained film we have a relationship, \( a_s = b_s < c_s \). Moreover, because the \( a_o \) and \( b_o \) lattice constants of the films are not equal, the pseudocubic lattice will be tilted from the [001]_o axis by an angle \( \gamma_c \neq 90^\circ \) (see Fig. 2). According to the Glazer notation, only one tilt system satisfies all these conditions: \#9 (\( a' + a' - c' \)).\cite{glazer1972} Therefore, we can infer that our SRO and LSMO thin films under compressive stress possess a monoclinic unit cell with space group \( P2_1/m \) (No. 11) with \( d_m = \sqrt{a^2_c + c^2 - 2a_c c \cos \alpha_c} \), \( b_m = \sqrt{a^2_c + c^2 + 2a_c c \cos \alpha_c} \), \( c_m = 2a_c \), \( \alpha_m = \beta_m = 90^\circ \), and \( \gamma_m < 90^\circ \), which is in perfect agreement with our observations shown in Table I.

It is important to note that the NGO(110) substrate has in-plane lattice parameters that are slightly different and therefore the condition \( a_s = b_s \) is not perfectly valid here. In this case, where \( a_s \neq b_s < c_s \), a Glazer tilt system \#8 (\( a' + b' - c' \)) might be more appropriate. Both \#9 and \#8 tilt systems are very similar. The thin-film unit cells under these tilt systems are both monoclinic with the same space group \( P2_1/m \) (No. 11). The rotation pattern is also preserved under both tilt systems, except that in tilt system \#8 the \( \text{BO}_6 \) octahedra will be rotated with slightly different magnitudes around the [100]_o and [010]_o directions.

The schematic view of the \( \text{BO}_6 \) octahedra rotations under compressive stress is shown in Figs. 6(a) and 6(b). Octahedral rotations in thin films under compressive stress have different patterns around the orthogonal in-plane directions: around the [100]_o, direction the rotations are in phase, while rotations around the [010]_o, direction they are out of phase. The \( \text{BO}_6 \) octahedra are also rotated out of phase around the [001]_o direction.

D. \( \text{BO}_6 \) octahedra rotations under tensile stress

For the tensile stress we have a situation where \( a_s = b_s > c_s \) and \( \alpha_c = 90^\circ \). In order to allow pseudocubic \( a_s \) and \( b_s \) axes to become longer with respect to the \( c_s \) axis, octahedral rotations...
around the [001] direction have to be significantly reduced or absent. The XRD results show that for films under tensile stress, the \( a_o \) and \( b_o \) lattice constants exhibit similar values. We can therefore conclude that, during the transition from compressive to tensile strain, the rotations of \( BO_6 \) octahedra around the \( c_o \) axis are diminished while rotations around the \( a_o \) and \( b_o \) axes are still maintained. Such a rotation pattern can be expressed by a tilt system \#18 \((a^+a^-c^0)\), in which \( BO_6 \) rotations around the \( a_o \) and \( b_o \) axes are analogous to those under compressive stress, but are absent around the \( c_o \) axis. This tilt system results in a tetragonal unit cell with the lattice parameters \( a_o = b_o = a_c \), \( c_o = 2c_c \), and \( a_t = b_t = y_t = 90^\circ \), and is described by the space group \( Cmcm \) (No. 63).

The Glazer tilt system \#16 \((a^+a^-c^0)\) also satisfies the condition of a film under tensile stress, where \( a_o = b_o > c_o \) and \( a_c = 90^\circ \), and will also result in a tetragonal unit cell but with the space group \( 4/mmm \) (No. 139). In contrast to the tilt system \#18 \((a^+a^-c^0)\), \( BO_6 \) octahedra under the tilt system \#16 \((a^+a^-c^0)\) are rotated in phase around both \( [001] \) and \([010] \) in-plane directions. According to Woodward, the former tilt system, \#18 \((a^+a^-c^0)\), cannot be achieved without some deformations of \( BO_6 \) octahedra. In order to retain the connectivity of octahedra in this tilt system, either the variation of octahedra angles from 90° by \( \sim 0.3^\circ \) for 1/6 of the bonds or the deviation of B-O distance by \( \sim 0.002 \) Å for 1/3 of the bonds has to be considered. Both deformations are very small and cannot be observed either by XRD or EXAFS techniques. Because the tilt system \#18 \((a^+a^-c^0)\) involves such small deformations, we believe that this tilt system is more likely to occur in thin films under tensile stress than the tilt system \#16 \((a^+a^-c^0)\). The tilt system \#18 \((a^+a^-c^0)\) preserves the in-plane octahedral rotation pattern as the film goes from compressive to a tensile stress while the Glazer system \#16 \((a^+a^-c^0)\) requires a change in the rotation pattern of \( BO_6 \) octahedra, which might not be energetically favorable. The schematic view of the \( BO_6 \) octahedra rotations under tensile stress is shown in Figs. 6(c) and 6(d). Octahedral rotations in thin films under tensile stress have different patterns around the orthogonal in-plane directions: Around the \([001] \) direction the rotations are in phase, while rotations around the \([010] \) direction are out of phase. The rotations of the \( BO_6 \) octahedra around the \([001] \) direction are greatly diminished or absent. The degree of octahedral rotations around the \([010] \) and \([001] \) directions depends on the magnitude of a mismatch. No rotations should occur in coherently strained film if the substrate in-plane lattice constant exceeds the film’s B-O-B distance. In that case the B-O-B bond angle will be set at 180° and further strain accommodation most likely will be achieved by octahedral deformation. This will result in shorter out-of-plane B-O bond lengths as compared to the in-plane ones. So far we have not been able to determine with sufficient accuracy the Ru-O (in \( SrRuO_3 \)) and Mn-O (in \( La_{0.67}Sr_{0.33}MnO_3 \)) in-plane and out-of-plane bond lengths, and therefore cannot verify the deformations of RuO\(_6\) and MnO\(_6\) octahedra. The effect is still under investigation.

### E. EXAFS measurements

The tilts of \( BO_6 \) octahedra were also confirmed by the EXAFS. We used linearly polarized synchrotron radiation, which allowed us to probe in-plane and out-of-plane interatomic bonds independently. The \( R \)-space Fourier-transformed Mn \( K \)-edge EXAFS spectra of the LSMO thin films grown under compressive and tensile stresses on LSAT and STO substrates, respectively. Data are shown (a) only for in-plane bond contributions and (b) only for out-of-plane bond contributions. C and T refer to the Mn-O-Mn bond under compressive and tensile stresses, respectively.
stress have straighter out-of-plane Mn-O-Mn bonds than films under tensile stress. EXAFS peak intensities along the out-of-plane direction are mainly influenced by MnO$_6$ octahedra rotations around the [100], and [010], axes. It is important to note that the Mn-O bond lengths are roughly the same in all cases, supporting a rigid octahedra scenario.\(^{31}\)

F. Implications of BO$_6$ octahedra rotations on the magnetic and transport properties

Owing to strong spin-orbit coupling, octahedral rotations are expected to influence some of the magnetic properties of SRO and LSMO materials. Studies have been reported on the magnetic anisotropy in SRO (Refs. 32–36) and LSMO (Refs. 37–43) thin films. Generally, reports of the uniaxial magnetic anisotropy in SRO thin films grown on STO(001) substrates strongly point to the importance of a monodomain growth regime, even though the in-plane lattice of the STO substrates exhibits uniaxial magnetic anisotropy around the [100] direction, while the hard axis is aligned along the [001] direction of the SRO unit cell. The mechanism of the monodomain growth of SRO(110) thin films on STO(001) substrates was already established elsewhere.\(^{44}\) While the uniaxial magnetic anisotropy in monodomain SRO films grown on STO(001) has been linked to a crystalline anisotropy through octahedral rotations,\(^{33}\) the complete rotational pattern of the RuO$_6$ octahedra and the resulting symmetry of the SRO unit cell were not described. According to our study, the SRO unit cell grown on the STO(001) substrate exhibits a uniaxial stress and assumes a monoclinic [110]-out-of-plane oriented unit cell with a space group $P_2_1/m$.\(^{33}\) According to Glazer, the octahedral rotation pattern of such a unit cell is not the same as the [100], and [010], directions, as shown in Figs. 6(a) and 6(b). The difference breaks the symmetry along perpendicular in-plane directions and therefore might be the cause for the in-plane anisotropic magnetic properties in SRO films under compressive stress.

Single-domain LSMO thin films grown on NGO(110) and LSAT(110) substrates under compressive stress also exhibit in-plane uniaxial magnetic anisotropy.\(^{16,43}\) The magnetic easy axis of a monoclinic LSMO(110) thin film grown on a NGO(110) substrate was found to be along the [1-10], direction, while the hard axis is aligned along the [001], direction.\(^{43}\) Besides a dissimilar in-plane MnO$_6$ octahedra rotation pattern, the uniaxial anisotropy in LSMO and NGO thin films also can be linked to the in-plane strain asymmetry arising from different in-plane lattice parameters of the NGO(110) substrate. The uniaxial magnetic anisotropy observed in LSMO films grown on LSAT(110) substrates cannot be attributed to the in-plane strain anisotropy because the in-plane lattice constants of a substrate are virtually the same.\(^{16}\) It was shown that thin LSMO(110) films grown on LSAT(110) substrates exhibit uniaxial magnetic anisotropy with an easy axis aligned along the [001], direction and a hard axis aligned along the [1-10], direction, which can only be explained by a distinct MnO$_6$ octahedra rotation pattern around perpendicular in-plane directions of a monoclinic unit cell (space group $P_2_1/m$).\(^{16}\) The uniaxial magnetic anisotropy was also observed in LSMO thin films grown on vicinal STO(001) substrates.\(^{40,45}\) Since it was shown above, the LSMO unit cell on STO(001) under tensile stress is tetragonal but with distinct octahedral rotations around perpendicular in-plane directions and no rotations around the [001], axis. The anisotropy in these films was reported to be step induced, and it is not apparent how the in-plane asymmetry of octahedral rotations influences anisotropy in these films.

The different octahedral rotations are expected to affect the orbital overlap and therefore modify transport properties of the films under different biaxial strains. In the case of SrRuO$_3$, a significant reduction of the conductivity was observed in thin films under tensile stress (tetragonal unit-cell symmetry) as compared to films under compressive stress (monoclinic unit-cell symmetry).\(^{24}\) The same behavior was observed in CaRuO$_3$ thin films as well. The preliminary studies of the transport properties in L$_{40.67}$ST$_{0.33}$MnO$_3$ thin-film samples show conductivities that are surprisingly similar between films grown on NGO, LSAT, and STO. More detailed studies are in progress.

G. Lattice modulations

We observed that LSMO thin films accommodate stress not only by BO$_6$ octahedra rotations. Under compressive stress thin films exhibit long-range lattice modulations.\(^{46}\) Figure 8 shows the reciprocal space maps of LSMO film grown on NGO taken around LSMO(hk0) Bragg reflections with $h = k = 1, 2, 3, 4$. Besides the Bragg peaks, satellite peaks are clearly visible. The satellite peaks are aligned in plane and their positions do not shift with the Bragg peak order, indicating that the satellites are originating from the long-range modulations, which are periodic in plane. Moreover, the satellites are only visible if the x-ray beam direction is parallel to the [001], unit-cell direction, and are absent along the [1-10], direction, demonstrating the highly anisotropic nature of the long-range modulations. Other groups also reported the existence of the satellite peaks in compressively strained LSMO thin films grown on LSAT substrates.\(^{47,48}\) Zhou et al. attributed the appearance of the satellites to the recovery of the rhombohedral LSMO unit cell as the thin film accommodates the mismatch stress by forming rhombohedral twins.\(^{47}\) Jin et al. reported domains consisting of monoclinic LSMO unit cells that form two domain motifs that give rise to the satellites.\(^{48}\) In both studies the rhombohedral and monoclinic unit cells were derived from the dissimilar positions of the asymmetric LSMO Bragg diffraction peaks along the [[001], [010], [1-10]], (-100], and [-0,10], in-plane directions. Interestingly, they observed that the satellite peaks were positioned either higher or lower in Q, value with respect to the positions asymmetric LSMO{103} Bragg peaks. If we overlook BO$_6$ octahedra rotations, our monoclinic (110)-oriented unit cell shown in Fig. 2 can be successfully described as a tilted pseudocubic (001)-oriented unit cell similar to the monoclinic one reported by Jin et al.\(^{48}\) However, in our case only (260),/(204), and (620),/(-204), peaks are at different positions while (444),/(024), and (44-4),/(0-24), peaks are at the same positions. Such a peak arrangement indicates that in our samples the pseudocubic unit cells are all tilted only along one direction, [1-10],/[010],, indicating the monodomain state. The results unequivocally show that twin domains in this case are not responsible for the satellite peak formation. Moreover, the tilt direction of the pseudocubic unit cell does not agree with the
direction of the long-range modulations. In fact, they are 90° apart in plane.

The observed results can be explained by assuming a monoclinic LSMO unit cell that is (110) out-of-plane oriented, as shown in Figs. 2 and 3. In bulk, besides the rhombohedral unit cell with the space group R-3c, the LSMO unit cell can be described as a monoclinic one with the symmetry group 22/c and the β angle slightly different from 90°.23 The variation of the β angle in the bulk unit cell alters the angle between the ab plane and the c axis. In thin films, as it was shown above, the coherent growth and the lattice mismatch constrains the unit cell into a monoclinic P21/m space group, where the γ angle deviates from 90° depending on the direction and the magnitude of the strain. Under compressive stress, as shown in Fig. 8(b), layers with such a unit cell exhibit lattice modulations only along the [001] direction. In contrast to the observations by Zhou et al. and Jin et al., satellite peaks in our films are perfectly aligned in plane with the asymmetric LSMO (444) and (44-4) Bragg peaks. No satellites were observed around the LSMO (260) and (620) peaks, whose in-plane positions are different by 90° from the LSMO(444) and (44-4) peaks as shown in Fig. 4. The origin of the modulations can be attributed to a deviation of an angle between the ab plane and the c axis of the monoclinic unit cell. The modulations can then be represented as the unit-cell displacements along the out-of-plane direction, which are periodic in plane along the [001] direction, similar to those described elsewhere.49–52

The existence of the satellite peaks along all the [100], [010], [-100], and [0-10], in-plane directions and their misalignment along Qz with respect to the Bragg peak positions observed by Jin et al. unambiguously indicate a presence of the 90° twinning of (110)-oriented monoclinic unit cells in LSMO films. It is interesting to note that Pailloux et al. observed twins in LSMO/STO layers only for the substrates with a very low miscut angle. For thin films on substrates with 1.5° miscut angle, twins were absent and only lattice modulations were visible. It was also reported that LSMO/STO thin films grown on vicinal substrates exhibit in-plane uniaxial magnetic anisotropy with the easy axis along the step-edge direction.40,45

The findings mentioned above point to the importance of the LSMO unit-cell orientation, which exhibits a different octahedral rotation pattern along the perpendicular in-plane directions to the magnetic properties of the LSMO thin films.

The observed lattice modulations can be quantitatively described using a kinematical XRD. For simplicity, in the model we used a pseudocubic cubic LSMO unit cell with \( a_{||} = c_{||} / 2 \) and \( a_{\perp} = (a_{||}^2 + b_{||}^2 - 2a_{||}b_{||} \cos(180° - \gamma_c)) / 2 \), where \( a_{||} \) and \( a_{\perp} \) are the in-plane and out-of-plane pseudocubic lattice parameters, respectively. We assume that the unit cells have displacements along the L direction (out of plane), which are periodic along the H direction (in plane) with periodicity, \( \Lambda \). Then a one-dimensional complex structure factor along the H direction can be written as

\[
F_H = F_{uc} \sum_j e^{2\pi i (Hx_j + Lz_j)} = F_{uc} \sum_{n=1}^{N} \exp \left[ 2\pi i \left( \frac{Hx_n}{a_{||}} + \frac{Lz_n}{a_{\perp}} \right) \right],
\]

where \( F_{uc}, x_j = \frac{x_j}{a_{||}}, \) and \( z_j = \frac{z_j}{a_{\perp}} \) are the unit-cell structure factor and the relative x and z positions along the H and L directions of a LSMO pseudocubic unit cell, respectively. \( N \) is the total number of the unit cells along the H direction. We consider that the unit-cell displacements occur only along the L direction, and they are periodic only along the H direction, such that \( x_n = n a_{||} \) and \( z_n = A_L \cos(k_H n a_{||}) \), where \( n \) is a unit-cell number, \( A_L \) is the modulation amplitude, and \( k_H = \frac{2\pi}{\Lambda} \) is a modulation wave vector. In this case the structure factor can be rewritten as

\[
F_H = F_{uc} \sum_{n=1}^{N} \exp \left[ 2\pi i \left( H_n + \frac{L}{a_{\perp}} A_L \cos(k_H n a_{||}) \right) \right].
\]

In order to account for the satellite peak broadening, we assume that the modulation period deviates from a mean value \( \Lambda \) according to a Gaussian distribution with a standard deviation,
The simulation results, together with experimental data for LSMO/LSAT and LSMO/NGO samples, are shown in Fig. 9. As can be seen from the figure, the kinematical model was able to reproduce all features of the XRD spectra: main Bragg peak, satellite peak positions, and intensities and widths using single parameters; for LSMO/LSAT, $\Delta = 30$ nm, $A_L = 0.40$ Å, and $\delta \Lambda = 5$ nm, and for LSMO/NGO, $\Lambda = 23$ nm, $A_L = 0.18$ Å, and $\delta \Lambda = 5$ nm. The simulations were also performed assuming unit-cell displacements along the in-plane [1-10]$_c$ direction. However, it did not produce satisfactory results, indicating that unit-cell displacements occur only along the out-of-plane direction, which is consistent with the coherent layer growth on a single-crystal substrate. The highly anisotropic nature of the lattice modulations further confirms the statement that the stress is accommodated differently along the perpendicular in-plane directions in LSMO and SRO thin films.

**IV. CONCLUSIONS**

We have demonstrated that under epitaxial strain thin LSMO and SRO films behave very similarly: Under compressive stress they have a (110) out-of-plane oriented monoclinic unit cell with space group $P_2_1/m$ (No. 11), while under tensile stress both films exhibit a [001] out-of-plane oriented tetragonal unit cell with space group $Cnmc$ (No. 63). The out-of-phase octahedral rotations around the out-of-plane [001]$_c$ direction are present in thin films under compressive stress (monoclinic unit-cell symmetry) while in films under tensile stress (tetragonal unit-cell symmetry) such rotations are absent. In both cases $BO_6$ octahedra are rotated in phase around the [100]$_c$ direction and out of phase around the [010]$_c$ direction. The additional strain along the [001]$_c$ direction is accommodated by periodic lattice modulations. The changes in octahedral rotations owing to stress and the dissimilar in-plane rotational patterns affect some physical properties in these materials, such as conductivity in SRO thin films and in-plane magnetic anisotropy in LSMO films. We believe that the observed lattice response to the epitaxial strain is of a general nature and can be applied to other perovskite-type materials that possess bulk orthorhombic or rhombohedral structures.

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It is important to note that some thin films under tensile stress still exhibit a small difference in $a_{f}$ and $b_{o}$ axis lengths of $\sim$0.003–0.005 Å, indicating that slight octahedra rotations around the $c_{o}$ axis might still be present.

Owing to rather limited $k$ space (up to 10 Å$^{-1}$) we cannot exclude some MnO$_6$ octahedra distortions resulting from the difference in the Mn-O bond lengths.