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CENTRE EUROPÉEN DE RECHERCHE ET DE FORMATION AVANCÉE EN CALCUL SCIENTIFIQUE

Exploring strategies to exploit machine learning in HPC-CFD

Corentin Lapeyre MAGISTER • 2020.09.15

Acknowledgments: A. Misdariis, N. Cazard, C. Besombes, V. Xing, E. Gullaud, L. Drozda, T. Poinsot, M. Bauerheim (ISAE), R. Selmi (TOTAL) and many more contributors...



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Hype Cycle for Emerging Technologies, 2020



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Expectations













Intro

Expectations





Intro

Hype Cycle for Emerging Technologies, 2020



Expectations

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Intro



How is Data Science (DS) relevant to the Physical sciences? A.k.a. how do we separate the hype from what's truly useful?







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Machines that learn?



Statistics: The science of collecting, displaying, and analysing data oxfordreference.com







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Machine Learning

Data science

ex: estimators, correlation, unsupervised clustering...

Statistics: The science of collecting, displaying, and analysing data oxfordreference.com

Data mining and processing ex: estimators, correlation, **Statistical analysis** unsupervised clustering... **Machine learning** decision trees **Big data** artificial neural reinforcement learning networks rule based support vector machines genetic algorithms



Machine Learning

Data science

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Statistics: The science of collecting, displaying, and analysing data oxfordreference.com





Machine Learning

Data science

ex: estimators, correlation, unsupervised clustering...

Machine learning

supervised clustering

- reinforcement
- learning
- rule based
- genetic algorithms

Deep learning

Statistics: The science of collecting, displaying, and analysing data oxfordreference.com





Machine Learning

Data science

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Machine learning

supervised clustering

- reinforcement
- learning
- rule based
- genetic algorithms

Deep learning

The new cool kids **~** « Al »

M	U	tip	olie	CQ	tic	on	S	qı	Ja	re
X	ໂ	2	3	4	5	6	7	8	9	10
1	1	2	3	4	5	6	7	8	9	10
2	2	4	6	8	10	12	14	16	18	20
3	3	6	9	12	15	18	21	24	27	30
4	4	8	12	16	20	24	28	32	36	40
5	5	10	15	20	25	30	35	40	45	50
6	6	12	18	24	30	36	42	48	54	60
7	7	14	21	28	35	42	49	56	63	70
8	8	16	24	32	40	48	56	64	72	80
9	9	18	27	36	45	54	63	72	81	90
10	10	20	30	40	50	60	70	80	90	100

Learn by heart











Machine Learning

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Learn abstract concepts





Learn motor skills



Machine Learning

det (E-E. (Y,£,/

Learn abstract concepts

Boston Dynamics | TED









At it's heart: Bayesian Inference: (just like humans! [1])



Machine Learning

Hypothesis HEvidence E

$P(H|E) \propto P(E|H) \cdot P(H)$

At it's heart: *Bayesian Inference:* (just like humans! [1])



Machine Learning

Hypothesis HEvidence E

$P(H|E) \propto P(E|H) \cdot P(H)$ Prior

At it's heart: Bayesian Inference: (just like humans! [1])



Machine Learning

Hypothesis HEvidence E

$P(H|E) \propto P(E|H) \cdot P(H)$ Likelihood Prior

At it's heart: Bayesian Inference: (just like humans! [1])





Machine Learning

Hypothesis HEvidence E

$P(H | E) \propto P(E | H) \cdot P(H)$

Posterior

Likelihood

Prior

At it's heart: *Bayesian Inference:* (just like humans! [1])

• Procedure: Choose Prior (e.g. « linear relation ») o Compute Likelihood o Evaluate Posterior Repeat (with new Prior)

 Priori beliefs (H) are updated according to evidence (E), using Bayes' rule

Machine Learning

Hypothesis HEvidence E

$P(H|E) \propto P(E|H) \cdot P(H)$

Posterior

Likelihood

Prior

Often called « glorified curve-fitting »

<u>Objective</u>: find the prior beliefs (H) that lead to the best posterior



[1] Wolpert, David H. "The lack of a priori distinctions between learning algorithms." Neural computation 8.7 (1996): 1341-1390.
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Machine Learning

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Conclusion: my hypothesis is supported by the data, so I'm now more confident in it

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Often called « glorified curve-fitting »

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Conclusion: my hypothesis is supported by the data, so I'm now more confident in it

Conclusion: 🤡 The data doesn't support H

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Machine Learning



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[1] Wolpert, David H. "The lack of a priori distinctions between learning algorithms." Neural computation 8.7 (1996): 1341-1390. **E**CERFACS 11

Machine Learning


How about machine learning?

Often called « glorified curve-fitting »

<u>Objective</u>: find the prior beliefs (H) that lead to the best posterior



[1] Wolpert, David H. "The lack of a priori distinctions between learning algorithms." Neural computation 8.7 (1996): 1341-1390. **Z**CERFACS 11

Machine Learning

P(H|E)



35

Conclusion: Nothing works!

Some problems are ill-posed: There is a fundamental ambiguity that cannot be resolved



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Machine Learning





EXERFACS | 12 Breiman, L. (2001). Statistical modeling: The two cultures. *Statistical science*, 16(3), 199-231.

Machine Learning



The scientific method is historically a deductive approach. **The data validates the model.**



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Machine Learning



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ZCERFACS 12 Breiman, L. (2001). Statistical modeling: The two cultures. *Statistical science*, 16(3), 199-231.

Machine Learning

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Z CERFACS Breiman, L. (2001). Statistical modeling: The two cultures. *Statistical science*, 16(3), 199-231. 12

The scientific method is historically a deductive approach. The data validates the model.

Data-driven approaches are inductive. The model is the output.









Machine Learning

 Shiny « superhuman » algorithms make headlines







Machine Learning

 Shiny « superhuman » algorithms make headlines





- Shiny « superhuman » algorithms make headlines
- But most applications
 automate the boring stuff ».

Just like regular programming does!



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- Shiny « superhuman » algorithms make headlines
- But most applications « automate the boring stuff ».

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13

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One definition of intelligence: Intelligence = (from F. Chollet)

Skill



¹: Silver, D., Hubert, T., Schrittwieser, J., Antonoglou, I., Lai, M., Guez, A., ... & Lillicrap, T. (2017). Mastering chess and shogi by self-play with a general reinforcement learning algorithm.

Machine Learning

ntelligence = Skill Experience



One definition of intelligence: Intelligence = (from F. Chollet)

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Machine Learning

Intelligence = $\frac{Skill}{Experience}$



Alpha Zero¹ needs 21 Million games of Go during training **but** training takes ≈24h

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Machine Learning

Intelligence = $\frac{Skill}{Experience}$

If enough experience can be gained, ML eventually beats humans

Experience

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Finding a good ML problem

Focus on problems that would be difficult to solve with traditional programming



Machine Learning

Finding a good ML problem

Focus on problems that would be difficult to solve with traditional programming





Neural networks \approx « intuition machines ». If you can do it but you don't know how, you can't code it. Example:

Finding a good ML problem

Focus on problems that would be difficult to solve with traditional programming



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Finding a good ML problem

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Know the problem before focusing on the data



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Neural networks \approx « intuition machines ». If you can do it but you don't know how, you can't code it. Example:



Finding a good ML problem

Focus on problems that would be difficult to solve with traditional programming

Know the problem before focusing on the data

Get lots of data



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Finding a good ML problem

Focus on problems that would be difficult to solve with traditional programming

Know the problem before focusing on the data

Get lots of data

Ok, but what is a lot?



Neural networks ≈ « intuition machines ». If you can do it but you don't know how, you can't code it. Example:



Finding a good ML problem

Focus on problems that would be difficult to solve with traditional programming

Know the problem before focusing on the data

Get lots of data

Don't let ML do the hard work of choosing features



Neural networks \approx « intuition machines ». If you can do it but you don't know how, you can't code it. Example:



Where's the cat?

Ok, but what is a lot?

How much data?





Low intelligence + low experience = low skill

How much data?



https://scikit-learn.org/





Low intelligence + low experience = low skill

















How much data?

0 ≈ 30 100-1000

Statistical tests (χ^2 ...)

<u>;;;</u>

Simple regression very low dimension Regression, SVMs, Trees, Ensemble methods ...



Machine Learning

100,000

Neural Network territory

Data

Not enough data ... ?

Earthquake frequency: The Gutenberg-Richter Law



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N. Silver, The Signal and the Noise, 2012

Not enough data ... ?

Earthquake frequency: The Gutenberg-Richter Law



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N. Silver, The Signal and the Noise, 2012

Not enough data ... ?

Earthquake frequency: The Gutenberg-Richter Law



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Machine Learning



N. Silver, The Signal and the Noise, 2012
Not enough data ... ?

Earthquake frequency: The Gutenberg-Richter Law



1 every 1000 years 1



Machine Learning



Not enough data ... ?





1 every 100 years

Magnitude *M*



Machine Learning



Not enough data ...?





1 every 100 years

Magnitude M



Machine Learning



Not enough data ...?



1 every 100 years

1 every ~ 300 years



Machine Learning



Case Studies of Al in CFD





















































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Larger timesteps

 Many degrees of AI « intrusion » in CFD are possible It is not yet clear which is the best way to go! **E**CERFACS 20



Larger timesteps

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Larger timesteps

 Many degrees of AI « intrusion » in CFD are possible It is not yet clear which is the best way to go! **E**CERFACS 20



1. Subgrid-scale modeling with CNNs

Ongoing PhD of Victor Xing, Cerfacs

Lapeyre, C.J., Misdariis, A., Cazard, N. & Poinsot, T (2018). A-posteriori evaluation of a deep convolutional neural network approach to subgrid-scale flame surface estimation. Proc. CTR Summer Program, 349-358.

Lapeyre, C.J., Misdariis, A., Cazard, N., Veynante, D. & Poinsot, T. (2019). Training convolutional neural networks to estimate turbulent sub-grid scale reaction rates. Combustion and Flame, 203, 255-264





Very large scale combustion







Elsa Gullaud, Post-Doc 2019

Very large scale combustion







Elsa Gullaud, Post-Doc 2019

What I can pay for





THE LOCAL PARTY IN THE PARTY INTO THE P





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THE LOCAL PARTY IN THE PARTY INTO THE P

























ML / DL based model for onthe-fly use



Combustion SGS



 $\mathbf{\Sigma} \mathbf{CERFACS} \mid 24 \qquad [1] \text{ Butler, T. D. & O'}$

[1] Butler, T. D. & O'Rourke, P. J. (1977). Symp. (Int.) Combust. 16, 1503 – 1515.





Combustion SGS



ECERFACS 24

[1] Butler, T. D. & O'Rourke, P. J. (1977). Symp. (Int.) Combust. 16, 1503 – 1515.



<u>DNS:</u> Resolved flame

<u>LES:</u> *e.g.* Artificially thickened flame [1]

Efficiency functions f - local to global

LOCAL FORMULATIONS:

- 1989 Gouldin (fractal)
- 2000 Colin *et al.*
- 2002 Charlette et al.



$\Xi:\mathbb{R}^k\mapsto\mathbb{R}$





Efficiency functions f - local to global

LOCAL FORMULATIONS:

- 1989 Gouldin (fractal)
- 2000 Colin *et al.*
- 2002 Charlette et al.

DYNAMIC FORMULATIONS:
 2011 - Wang *et al.*



$\Xi:\mathbb{R}^k\mapsto\mathbb{R}$



$\Xi: \mathbb{R}^{2k} \mapsto \mathbb{R}$





Efficiency functions f - local to global

LOCAL FORMULATIONS:

- 1989 Gouldin (fractal)
- 2000 Colin *et al.*
- 2002 Charlette et al.

DYNAMIC FORMULATIONS: <a>2011 - Wang *et al.*

CNN FORMULATION: 2019 - Lapeyre *et al.*



$\Xi:\mathbb{R}^k\mapsto\mathbb{R}$



$\Xi: \mathbb{R}^{2k} \mapsto \mathbb{R}$



Building the dataset



Convolutional neural network



Neural network

Input



Segmented image



Architecture is adapted from a medical image segmentation network [9]



27 Ronneberger, O., Fischer, P., & Brox, T. (2015, October). U-net: Convolutional networks for biomedical image segmentation. In *International Conference on Medical image computing and computer-assisted intervention* (pp. 234-241). Springer, Cham.



Neural network





Neural network





Receptive field
Neural network





Receptive field

Neural network





Receptive field

Neural network



• Network is trained on increasing size inputs: 8³, then 16³, and finally 32^3 .

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Receptive field

Training setup



















Training setup















С

Training setup















DNS for training



Numerical simulation of a laboratory-scale turbulent slot flame. *Proceedings of the combustion* 30 *institute*, *31*(1), 1299-1307.

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Similar to: Bell, J. B., Day, M. S., Grcar, J. F., Lijewski, M. J., Driscoll, J. F., & Filatyev, S. A. (2007).

A priori test

Test case: unsteady flow dynamics



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 $u_{in} [m/s]$





A priori results



Example snapshot during test



A priori results



Example snapshot during test



Excellent agreement compared to litterature.

A posteriori strategy

Training setup







CNN















A posteriori strategy

Training setup







CNN



Target setup





AVBP DNS





AVBP-DL LES



tailed parison

Tests a posteriori in LES:

- The CNN can be integrated in AVBP code to compute flame wrinkling but the inference time (evaluation of f_{CNN}) becomes too long on CPU: GPUs are much better
- -> hybrid architecture is needed



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CPU : Navier-Stokes solver (AVBP)





GPU : CNN (TensorFlow)

Tests a posteriori in LES:

• The CNN can be integrated in AVBP code to compute flame wrinkling but the inference time (evaluation of f_{CNN}) becomes too long on CPU: GPUs are much better -> hybrid architecture is needed



models on this setup



models on this setup



JZ Grand Challenge

- We target large scale LES => hybrid CPU/GPU and solver/neural network approach must scale to HPC
- 2019-2020: Jean Zay Grand Challenge

AVBP-DL: 2000 CPU + 64 GPU simulation on Jean Zay





V. Xing (Ph.D. started 2019), supervised by C. Lapeyre, A. Misdariis, O. Vermorel & T. Poinsot





V. Xing, A. Misdariis, G. Staffelbach, C. Lapeyre



2. Data-driven discretization



Ongoing PhD of Luciano Drozda, Cerfacs















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- One of the less intrusive approaches
- Objective: achieve better gradient estimation on coarse meshes $\langle = \rangle$ run same simulation on coarser mesh



- One of the less intrusive approaches
- Objective: achieve better gradient estimation on coarse meshes $\langle = \rangle$ run same simulation on coarser mesh

Data Driven Discretization Spatial derivatives Cell average at $\frac{\partial^{\ell} u(x_n)}{\partial x^k} = \sum \alpha_{nm}^{(\ell)} u(x_{n-m})$ time t $u(x_n)$ Flux (equation specific) $J(x_n) = J\left(x_n, u(x_n), \frac{\partial}{\partial x}u(x_n), \frac{\partial^2}{\partial x^2}u(x_n), \ldots\right)$ Time derivative Cell average at time $t+\Delta t$ $\frac{\partial u(x_n)}{\partial t} = -\frac{1}{\Delta x} \left[J\left(x_{n+\frac{1}{2}}\right) - J\left(x_{n-\frac{1}{2}}\right) \right]$ (method of lines)



- One of the less intrusive approaches
- Objective: achieve better gradient estimation on coarse meshes $\langle = \rangle$ run same simulation on coarser mesh



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 $\mathbf{\Sigma} \mathbf{CERFACS} \mid 40$

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 $\mathbf{\Sigma} \mathbf{CERFACS} \mid 40$

Ongoing PhD of Luciano Drozda, Cerfacs

Great idea, difficult execution

- Challenge #1: differentiability • NN require the chain to be differentiable *i.e.* you must rewrite your CFD solver in a deep learning framework
 - Several solvers with this tech under development (e.g. PhiFlow [1] at TUM)
- Challenge #2: time stability
 - Supervised learning (error wrt next iteration) leaves room for small errors that accumulate => divergence
 - BUT training in a supervised manner long term doesn't seem to work: turbulent paths differ, and punishing the network for difference to DNS doesn't work anymore

ECERFACS 41 [1] https://ge.in.tum.de/research/phiflow/

Concluding remarks




































































Hybrid Physical HPC Solvers







PDE solvers (CPU) coupled with NN inference (GPU)









Distribution Parametrization

Generative

Hybrid Physical HPC Solvers







PDE solvers (CPU) coupled with NN inference (GPU)















Thank you

• <u>Papers:</u>

- Lapeyre, C.J., Misdariis, A., Cazard, N., Veynante, D. & Poinsot, T. (2019). Training convolutional neural networks to estimate turbulent sub-grid scale reaction rates. Combustion and Flame, 203, 255-264.
- <u>Conferences:</u>
 - Lapeyre, C. J., Cazard, N., Roy, P. T., Ricci, S., & Zaoui, F. (2019). Reconstruction of Hydraulic Data by Machine Learning. SimHydro 2019, Nice, France, June 12-14, arXiv:1903.01123.
 - Lapeyre, C.J., Misdariis, A., Cazard, N., Xing, V., Veynante, D. & Poinsot, T. (2019). A convolutional neural network-based efficiency function for sub-grid flame-turbulence interaction in LES. 16th International Conference on Numerical Combustion, May 6-8 2015, Avignon France.
 - Ronan Paugam, Melanie Rochoux, Nicolas Cazard, Corentin Lapeyre, William Mell, Joshua Johnston, and Martin Wooster: Computing High Resolution Fire Behavior Metrics from Prescribed Burn using Handheld Airborne Thermal Camera Observations. The 6th International Fire Behaviour and Fuels Conference, Marseilles, May 2019.
 - Ronan Paugam, Melanie Rochoux, Nicolas Cazard, Corentin Lapeyre, William Mell, Joshua Johnston, and Martin Wooster. Journée de télédétection et incendie Organisée par IRSTEA, Aix, Decembre 2018.
 - Lapeyre, C.J., Misdariis, A., Cazard, N, Poinsot, T. Replacing a sub-grid closure model with a trained deep convolutional neural network. HiFiLeD Symposium, November 14-16th 2018, Brussels Belgium.
- <u>Other:</u>
 - Lapeyre, C.J., Misdariis, A., Cazard, N. & Poinsot, T (2018). A-posteriori evaluation of a deep convolutional neural network approach to subgrid-scale flame surface estimation. Proc. CTR Summer Program, 349-358.

